

TRAJ--A Two Dimensional Trajectory Program For Personal Computers*

prepared by

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ABSTRACT

The computer code TRAJ was developed to allow relatively complex trajectory calculations to be performed on a desk top personal computer. The code includes the effects of projectile mass, shape, density, launch velocity, and launch angle, as well as multiple ricochets from the ground. Terrain effects, barricades, buildings, etc can also be defined and included in the calculations. The code is briefly described and sample problems and outputs are presented.

BACKGROUND

The computer program TRAJ was originally developed at the Naval Surface Warfare Center (NAVSWC) by Porzel as part of the Naval Explosives Safety Improvement Program (NESIP)¹. It is based on an analytic solution to the classical "v² drag" trajectory problem. Reference 1 provides the basic assumptions and equations around which the program is written. Over the past ten years (since the publication of Reference 1), developments and improvements have continued in the program. This paper presents the latest version of the program and discusses some of the changes which have been made to the program.

These developments include (but are not limited to): (1) terrain effects--sloping terrain, hills, valleys, etc., (2) the ability to "build" structures (barricades, buildings, etc) into the trajectory path, and (3) fragment ricochets from the ground or from structures. They also include various plotting and presentation options. The ricochet and structural interaction portions of the program were developed by the Boeing Military Airplane Company (Mr. Richard A. Lorenz), under contract to NAVSWC.

The ricochet methodology is based on work originally performed by the Army and incorporated into the computer program FRAGHAZ^{2,3}. When a fragment impacts the ground or a structure, its impact angle is compared with a critical ricochet angle to determine whether the fragment will ricochet. The critical ricochet angle is dependent on the type of soil. Once it is determined that the fragment will ricochet, the ricochet angle and velocity are determined from the incident angle and velocity as well as the soil type. When ricochet occurs, the trajectory calculation continues until no further ricochets occur and the fragment has come to rest.

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HARDWARE REQUIREMENTS

The program is written in BASIC and is designed to run on any IBM-compatible machine using DOS 3.1 operating system (or higher) with 640 kilobytes of memory and a hard disk. The program supports CGA, EGA, and VGA graphics. An IBM-AT (or faster) machine with math co-processor is highly recommended.

GENERAL

The input to the program is prepared interactively through a series of screens which question the user. At any time, the user may change his mind and replace information which has already been entered. The program is set up to operate in a modified English system of units. All lengths are in feet, areas in ft², and velocities in ft/s. All weights are in pounds. Fragment densities are in g/cm³. Impact energies are calculated in ft-lbs.

Several kinds of information are required to perform the calculations. The most important is a description of the fragment and the initial conditions. The fragment description includes mass, shape, and density. Mass and density are straightforward. The shape is not. The shape of an object is described by its shape factor, length in direction of motion, and cross sectional area. The shape factor is a required input, and is described below. Length in direction of motion, or cross sectional area can be entered as an option; but not both.

Shape Factor. The shape factor can be thought of as the ratio of the volume of the fragment to the volume of a rectangular box with the minimum dimensions required to hold the fragment. Typical explosively-formed fragments have shape factors around 0.333. Pre-formed fragments have a shape factor of 1.000. A sphere has a shape factor of $\pi/6$ (0.524). Experimentally-determined shape factors for concrete debris have ranged from 0.33 to 0.44.

Length in Direction of Motion. This is directly what it seems. If, for instance, it is known or postulated that a fragment flies like a spear, then the total length of the fragment would be the length in the direction of motion. In the program, this is referred to as Characteristic Fragment Length.

DESCRIPTION OF INPUT SCREENS

MAIN MENU

See Figure 1. Upon entering the program, you will see the Main Menu. It defines the six possible decision paths which are allowed within the program.

The first time a particular problem is run, Item 1 should be selected. This will lead to further screens which will be discussed later.

After Item 1 is completed, the trajectories are automatically calculated and stored on the hard disk. At this point, the Main Menu reappears. Here, a screen plot of the trajectories can be displayed through the use of Item 3. Item 4 presents a summary table of the final conditions for each of the trajectories computed. Item 5 presents details of the complete trajectory for each case. Item 2 is used to preview barrier or structure data before trajectory calculations are done (see THIRD INPUT SCREEN). It simply plots the terrain and any associated structures or barriers--but no trajectories. Item 6 causes the program to exit back to DOS.

Let us assume that Item 1 was initially selected.

FIRST INPUT SCREEN

See Figure 2. The program first reads an input data file "TRAJ.IN" from the hard disk. This file contains all of the trajectory input conditions that were used on the last Traj run. If you copy this file in DOS to another name, you can preserve these input conditions for future use, and copy them back to "TRAJ.IN" when needed. If the information on the screen is correct, answer Y to the question "Is this screen O.K. (Y/N)?" If the information requires modification, answer N.

The program is setup to do many trajectory calculations at one time using different initial velocities, angles, and masses. If you have answered N, the first information requested is the initial velocity: beginning, ending, and increment. The beginning and ending initial velocities are obvious. The increment may be either positive or negative. The beginning initial velocity is incremented by the amount chosen until the ending initial velocity is obtained (or exceeded). Thus a series of initial velocities can easily be chosen. The pointer is moved by use of the "Enter" key. If an item does not need to be changed, pressing "Enter" will accept the default value shown.

The second set of required data is the initial angle. This works in exactly the same way as the initial velocity. It must be remembered that each angle selected will be run with all initial velocities selected.

The third item required is the mass (or masses) of the fragments. This is simply a list of all the masses of interest (separated by an "Enter"). Up to 20 masses may be chosen. It should be noted that if the user chooses 10 initial velocities, 10 initial angles, and 10 masses, the program will calculate 1000 trajectories, which will take quite a long time (> 60 minutes). Also a screen plot of these would be far too crowded to allow interpretation.

The final item on this screen is the density of the fragments. If the material is one of the default materials, simply enter the corresponding number and press "Enter". Otherwise, choose "other" and enter the appropriate density.

When this is completed the prompt "Is this screen O.K. (Y/N)?" will appear. If all the information showing on the screen is correct, type Y. Then type space bar to continue to the next screen or M to return to the main menu (use this also if you want to return to a previous screen). If any of the information is still not correct, type N. This will allow you to cycle through the information on that screen again, changing anything needed.

SECOND INPUT SCREEN

See Figure 3. Again, the first thing encountered will be the dialog: "Is this screen O.K. (Y/N)?". To make changes on this screen, type N.

Select a shape factor from one of the options listed or choose other and enter the value.

If desired enter either the cross sectional area or the characteristic length (but not both), and enter zero for the other. If both are entered, the cross sectional area entered will be ignored.

If the trajectory is to be calculated for conditions other than at sea level, then the value of the atmospheric density and sound speed for that altitude will be required.

The fragment starting height allows the trajectory to start somewhere other than at ground level.

A drag coefficient table versus Mach number table is built into the program and is presented on this screen. The table is in terms of Drag Coefficient vs. Mach Number. Two choices are available with this table. The first asks whether interpolation between table entries is requested. If No is selected, the drag coefficient remains constant between Mach number entries. For example, the drag coefficient is assumed to be 0.8 for Mach numbers between 0.0 and 0.75, and 0.88 for 0.75 to 0.9, etc. If Yes is selected, the drag coefficient varies linearly from 0.8 to 0.88 for Mach numbers between 0.0 and 0.75, etc. The second choice allows direct change or modification to the table itself.

Again, when this is completed the prompts "Is this screen O.K. (Y/N)?" and "Type space bar to continue or M to return to main menu" will appear. If all the information showing on the screen is correct, type Y. Then type space bar to continue to the next screen. If any of the information is still not correct, type N. This will allow you to cycle through the information on that screen again, changing anything needed.

THIRD INPUT SCREEN

See Figure 4. This screen defines the terrain and any structures or barriers.

The first item is the minimum altitude. This defines a "lower limit altitude", below which calculations will not be carried out. This can be used for flat ground, but ricochet will not occur.

Next, you are asked if you would like to view the table of soil constants. These are required for the ricochet calculations. This table simply presents descriptions of the soil and their associated constants. It is shown in Figure 5. This is helpful in selecting the proper values.

Finally you are asked to define the terrain and barriers/structures. These are defined

by the coordinates (x,y) of points on the terrain or structure. The terrain is built up in segments—three pairs of points per segment. If only two points are given for a segment, a straight line is fitted between them. If three points are given for a segment, a quadratic is fitted. A soil constant is also required for each segment. If a value of 0 is put in for the soil constant, no ricochets will be allowed over that segment. Up to 10 segments are allowed.

Again, when this is completed the prompts "Is this screen O.K. (Y/N)?" and "Type space bar to continue or M to return to main menu" will appear. If any of the information is still not correct, type N. This will allow you to cycle through the information again, changing anything needed. If all the information showing on the screen is correct, type Y. Then type space bar. The program counts as each trajectory calculation is completed. When all of the calculations are completed, the input data file "TRAJ.IN" is written to disk.

Suppose that you have put in the coordinates of a terrain/barrier system and you wish to preview them before performing the calculations. In that case, instead of typing space bar to continue, type M and return to the Main Menu. On the main menu, select option 2 ("Plot Working Barrier Data"). This will produce a screen plot of the information provided. If it is correct, Enter option 1, and then choose Y on each screen. If the terrain/barrier is not correct, when Screen 3 appears, make the appropriate changes.

When the trajectory computations are completed, you are returned to the Main Menu.

GETTING A PRINTOUT OF SCREEN PLOTS

To obtain a printout of working barrier or fragment trajectory plots, type the DOS command "graphics" before running TRAJ. Then when a plot is displayed on the screen, press the "print screen" key and a copy of the screen will be sent to the printer. Some versions of DOS do not support "print screen" for VGA graphics, so in this case select EGA graphics when doing screen plots.

SAMPLE CALCULATIONS

Let us consider two problems. Each will be described. Then samples of the input screens and the outputs will be presented.

PROBLEM 1 (Figures 2 - 8)

Trajectories are calculated for a 20 pound concrete fragment. Initial velocities are 200 and 300 ft/s at angles of 30, 40, and 50 degrees above the horizontal. The terrain slopes downward from the source 50 feet in 800 feet to the base of a hill. The rounded hill peaks at 150 feet above the source at a distance of 1300 feet. The hill descends to level terrain 55 feet below the source at a distance of 1750 feet. The soil type is dry sand. Ricochet is enabled, but does not occur.

This problem illustrates: (1) the reversal of fragment range after maximum range is achieved; (2) trajectory termination on a downward slope, or linear barrier; (3) trajectory termination on a curved contour, or quadratic barrier; and (4) construction of a complex ground contour by connecting linear and/or quadratic segments.

PROBLEM 2 (Figures 9 - 15)

Trajectories are calculated for a 20 pound concrete fragment. Initial velocities are 200 and 300 ft/s at angles of 5, 7.5, and 10 degrees above the horizontal. The terrain slopes upward from the source 35 feet in 500 feet to a level plateau 200 feet in length. The terrain then returns to source level at a distance of 890 feet from the surface. A 4.4 foot vertical barrier is located about three-quarters of the way up the initial slope. The soil type is dry sand. Ricochet is enabled.

This problem illustrates: (1) ricochet on both ascending and descending slopes; (2) multiple ricochets for a single trajectory; (3) trajectory termination on a vertical barrier.

SUMMARY

The above examples illustrate the versatility of TRAJ, with its ability to handle uneven terrain with multiple barriers, its incorporation of ricochet, and its ability to calculate multiple trajectories with a range of input conditions in one run.

REFERENCES

1. Porzel, F. B., "Technology Base of the Navy Explosives Safety Improvement Program," Minutes of the Nineteenth Explosives Safety Seminar, Los Angeles, CA, 9-11 September 1980.
2. McCleskey, F., "Fragmentation Hazard Computer Model," Minutes of the Twenty-First Explosives Safety Seminar, Houston, TX, 28-30 Aug 1984.
3. McCleskey, F., "Quantity-Distance Fragment Hazard Computer Program (FRAGHAZ)," NSWC TR 87-59, February 1988.

Figure 1: MAIN MENU

MAIN MENU

1. CHANGE INPUT CONDITIONS, CALCULATE NEW TRAJECTORIES
2. PLOT WORKING BARRIER DATA
3. PLOT FRAGMENT TRAJECTORIES
4. DISPLAY FINAL CONDITIONS FOR FRAGMENTS
5. DISPLAY COMPLETE TRAJECTORY CONDITIONS FOR FRAGMENTS
6. EXIT PROGRAM

ENTER SELECTION NUMBER AND PRESS ENTER

Figure 2: FIRST INPUT SCREEN - PROBLEM 1

FRAGMENT TRAJECTORY DATA INPUT

| | BEGINNING | ENDING | INCREMENT |
|---------------------------|-----------|--------|-----------|
| INITIAL VELOCITY (FT/SEC) | 200 | 300 | 100 |
| INITIAL ANGLE (DEG) | 30 | 50 | 10 |

LIST OF MASSES (LB) SELECT FRAGMENT DENSITY (gm/cm³)

| | |
|----|--|
| 20 | 1. STEEL 7.8 |
| | 2. ALUMINUM 2.7 |
| | 3. CONCRETE > 2.4 < |
| | 4. CAST IRON 7.1 |
| | 5. OTHER — |

IS THIS SCREEN O.K. (Y/N) ?

Figure 3: SECOND INPUT SCREEN - PROBLEM 1

| | | | |
|--|---------|--|------|
| SELECT FRAGMENT SHAPE FACTOR | | INTERPOLATE THE DRAG COEFFICIENT TABLE (Y/N) Y | |
| 1. TYPICAL FRAGMENTS | 0.333 | | |
| 2. PREFORMED FRAGMENTS | 1.0 | | |
| 3. OTHER | > .46 < | | |
| DO YOU WANT TO CHANGE THE DRAG COEFFICIENT MACH NUMBER TABLE (Y/N) N | | | |
| FRAGMENT AREA (SQFT) | | | |
| (Enter Zero when Area is Unknown) 0 | | 1.08 | 4 |
| | | 1.14 | 2 |
| | | 1.26 | 1.15 |
| CHARACTERISTIC FRAGMENT LENGTH (FT) | | 1.09 | .9 |
| (Enter Zero when Length is Unknown) 0 | | .88 | .75 |
| | | .8 | 0 |
| AMBIENT DENSITY (LBS/CUFT) .07647 | | | |
| AMBIENT SOUND SPEED (FT/SEC) 1116.45 | | | |
| FRAGMENT STARTING HEIGHT (FT) 0 | | | |
| IS THIS SCREEN O.K. (Y/N) ? | | | |

Figure 4: THIRD INPUT SCREEN - PROBLEM 1

| | | | | | | | | | |
|---------------------------------------|--------------------|--------------------------|--------------------------------------|------------|-----------------------------|-----------------------------|---|---|-----|
| GROUND/TERRAIN AND BARRIER DATA INPUT | | | | | | | | | |
| MINIMUM ALTITUDE (FT) -60 | | | VIEW TABLE OF SOIL CONSTANTS (Y/N) N | | | | | | |
| NO. | 1ST POINT I PTS | 2ND POINT X(FT) Y(FT) | 3RD POINT X(FT) Y(FT) | SOIL CONST | ... Y = A*X^2 + B*X + C ... | | | | |
| I | PTS | X(FT) | Y(FT) | X(FT) | Y(FT) | A | B | C | 0-4 |
| 1 | 2 | 0 0 | 800 -50 | 2.00 | +.000D+00-.625D-01+.000D+00 | | | | |
| 2 | 3 | 800 -50 | 900 -45 | 1000 0 | 2.00 | +.200D-02-.335D+01+.135D+04 | | | |
| 3 | 3 | 1000 0 | 1300 150 | 1600 0 | 2.00 | -.167D-02+.433D+01-.267D+04 | | | |
| 4 | 3 | 1600 0 | 1700 -45 | 1750 -55 | 2.00 | +.167D-02-.595D+01+.525D+04 | | | |
| IS THIS SCREEN O.K. (Y/N) ? | | | | | | | | | |

Figure 5: TABLE OF SOIL CONSTANTS

SOIL CONSTANTS

| | |
|--------------------------------|-------------------------|
| HARD GREY CLAY | 0.07, 0.47 |
| WET EARTHWORK | 0.11 |
| EARTHWORK | 0.13 |
| WET CLAY | 0.16 |
| SOFT YELLOW CLAY | 0.24 - 0.27, 0.66, 1.09 |
| DAMP CLAY | 0.39 |
| CLAY-SOIL, SAND CLAY EARTHWORK | 0.53 |
| CLAY-SAND GRAVEL | 0.70 |
| GRASSY EARTHWORK | 0.81 |
| SAND GRAVEL | 1.67 |
| DRY SAND | 1.71 - 2.07 |
| EARTH-SAND GRAVEL | 2.24 |
| SAND | 2.91 - 4.0 |

PRESS ANY KEY TO CONTINUE

Figure 6: FINAL CONDITIONS DISPLAY - PROBLEM 1

| TRAJ ANGLE (DEG) | PATH LENGTH (FT) | HORIZ. RANGE (FT) | HEIGHT (FT) | ENERGY (FT-LBS) | VELOCITY (FT/SEC) | TIME (SEC) |
|-------------------------------|------------------------|-------------------------|--|--------------------|----------------------|---------------|
| INITIAL VEL. = 200 -44.797 | MASS = 20 857.394 | 784.364 | INITIAL ANGLE =30.000 # RICOCHETS = 0 -49.023 | 0.576D+04 | 136.094 | 6.10608 |
| INITIAL VEL. = 200 -54.947 | MASS = 20 966.240 | 820.719 | INITIAL ANGLE =40.000 # RICOCHETS = 0 -52.249 | 0.594D+04 | 138.215 | 7.48030 |
| INITIAL VEL. = 200 -63.146 | MASS = 20 1024.297 | 780.609 | INITIAL ANGLE =50.000 # RICOCHETS = 0 -48.788 | 0.625D+04 | 141.850 | 8.61986 |
| INITIAL VEL. = 300 -36.976 | MASS = 20 1187.870 | 1110.118 | INITIAL ANGLE =30.000 # RICOCHETS = 0 89.908 | 0.645D+04 | 144.107 | 6.60515 |
| INITIAL VEL. = 300 -50.089 | MASS = 20 1345.817 | 1170.052 | INITIAL ANGLE =40.000 # RICOCHETS = 0 121.856 | 0.633D+04 | 142.693 | 8.34218 |
| INITIAL VEL. = 300 -62.415 | MASS = 20 1486.509 | 1142.034 | INITIAL ANGLE =50.000 # RICOCHETS = 0 108.411 | 0.708D+04 | 150.916 | 10.14341 |

DO YOU WISH TO SEE THE OUTPUT AGAIN (Y/N) ?

Figure 7: PLOT OF WORKING BARRIER DATA - PROBLEM 1

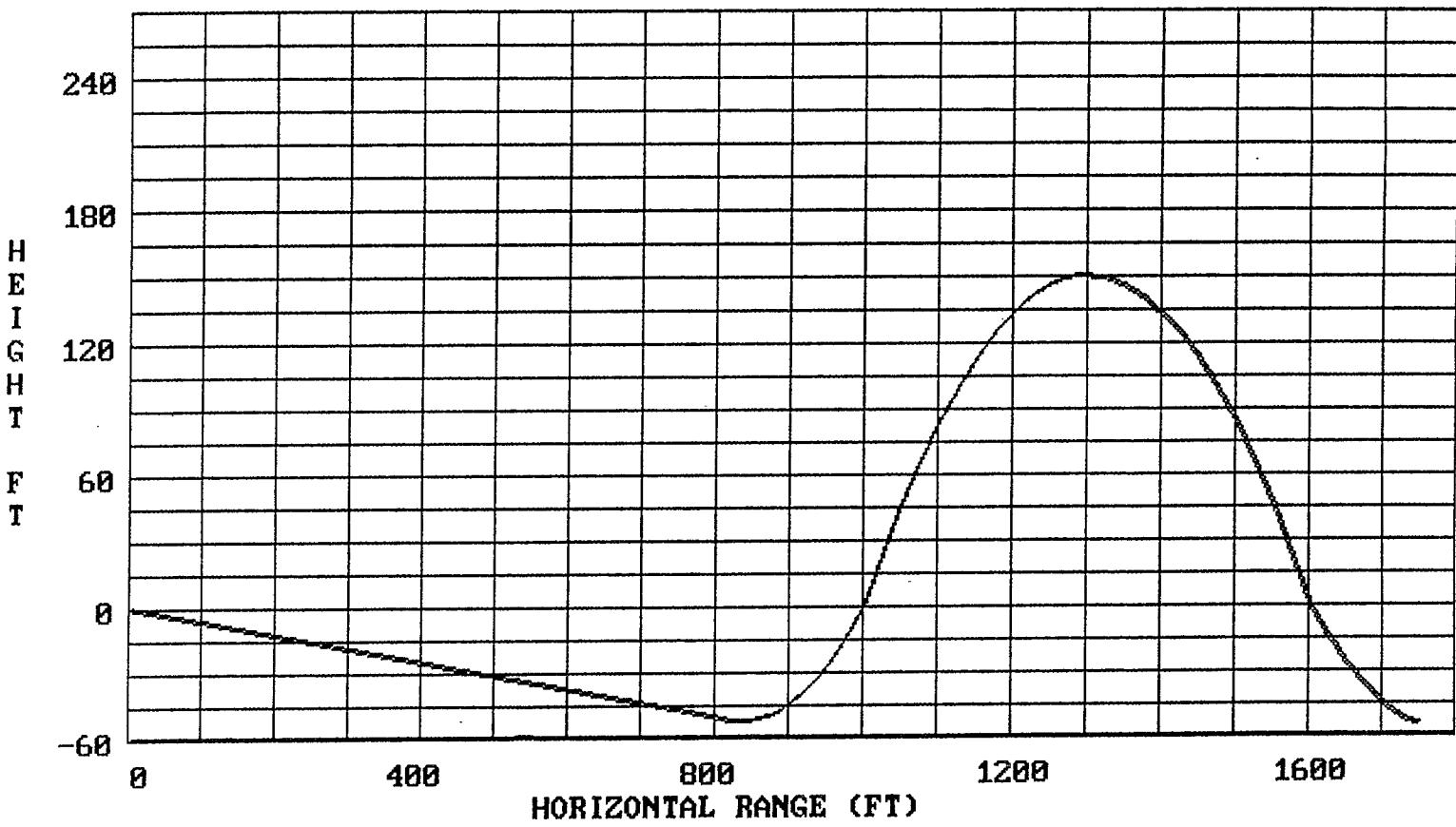


Figure 8: PLOT OF FRAGMENT TRAJECTORIES - PROBLEM 1

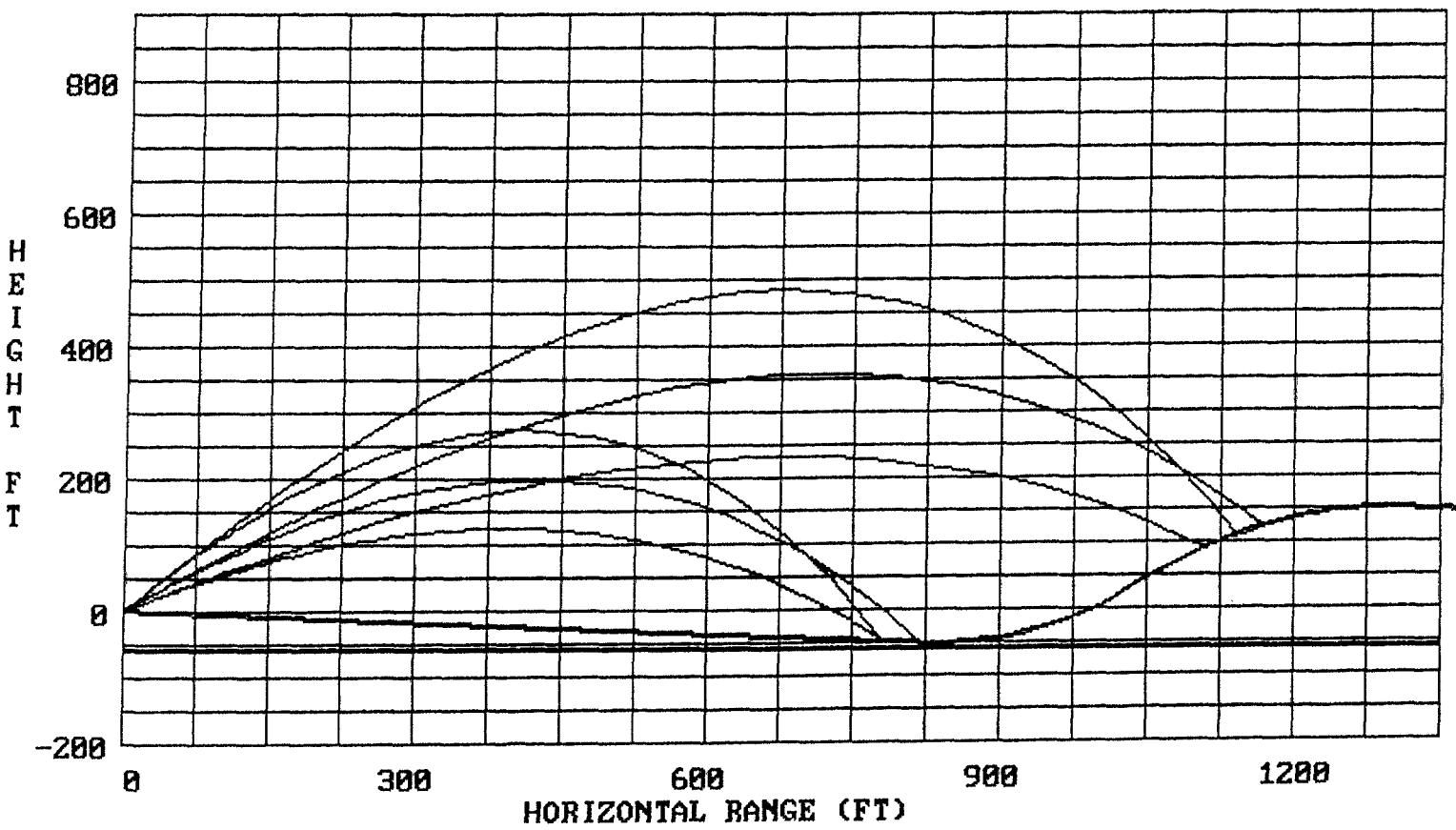


Figure 9: FIRST INPUT SCREEN - PROBLEM 2

| FRAGMENT TRAJECTORY DATA INPUT | | | |
|--------------------------------|--|-----------------------------------|-----------|
| | BEGINNING | ENDING | INCREMENT |
| INITIAL VELOCITY (FT/SEC) | 200 | 300 | 100 |
| INITIAL ANGLE (DEG) | 5 | 10 | 2.5 |
| LIST OF MASSES (LB) | SELECT FRAGMENT DENSITY (gm/cm ³) | | |
| 20 | 1. STEEL 2. ALUMINUM 3. CONCRETE 4. CAST IRON 5. OTHER | 7.8 2.7 > 2.4 < 7.1 — | |
| IS THIS SCREEN O.K. (Y/N) ? | | | |

Figure 10: SECOND INPUT SCREEN - PROBLEM 2

| | | | | |
|--|--|--|------|--|
| SELECT FRAGMENT SHAPE FACTOR | INTERPOLATE THE DRAG COEFFICIENT TABLE (Y/N) Y | | | |
| 1. TYPICAL FRAGMENTS 0.333 | | | | |
| 2. PREFORMED FRAGMENTS 1.0 | | | | |
| 3. OTHER >.46 < | | | | |
| FRAGMENT AREA (SQFT) (Enter Zero when Area is Unknown) | 0 | DO YOU WANT TO CHANGE THE DRAG COEFFICIENT MACH NUMBER TABLE (Y/N) N | | |
| CHARACTERISTIC FRAGMENT LENGTH (FT) (Enter Zero when Length is Unknown) | 0 | 1.08 | 4 | |
| | | 1.14 | 2 | |
| | | 1.26 | 1.15 | |
| | | 1.09 | .9 | |
| | | .88 | .75 | |
| | | .8 | 0 | |
| AMBIENT DENSITY (LBS/ CUFT) .07647 | | | | |
| AMBIENT SOUND SPEED (FT/SEC) 1116.45 | | | | |
| FRAGMENT STARTING HEIGHT (FT) 0 | | | | |
| IS THIS SCREEN O.K. (Y/N) ? | | | | |

Figure 11: THIRD INPUT SCREEN - PROBLEM 2

GROUND/TERRAIN AND BARRIER DATA INPUT

| | | | | | |
|-----------------------|--------------------------------|------------------------------------|--------------------------|------------|----------------------------------|
| MINIMUM ALTITUDE (FT) | 0 | VIEW TABLE OF SOIL CONSTANTS (Y/N) | N | | |
| NO. | 1ST POINT I PTS X(FT) Y(FT) | 2ND POINT X(FT) Y(FT) | 3RD POINT X(FT) Y(FT) | SOIL CONST | ... Y = A*X^2 + B*X + C ... |
| 1 | 2 0 0 | 500 35 | 500 35 | 0-4 | 2.00 +.000D+00+.700D-01+.000D+00 |
| 2 | 2 500 35 | 700 35 | 700 35 | | 2.00 +.000D+00+.000D+00+.350D+02 |
| 3 | 2 700 35 | 890 0 | 890 0 | | 2.00 +.000D+00-.184D+00+.164D+03 |
| 4 | 2 380 26.6 | 380 31 | 380 31 | | 2.00 +.000D+00+.100D+31+.000D+00 |

IS THIS SCREEN O.K. (Y/N) ?

Figure 12: FINAL CONDITIONS DISPLAY - PROBLEM 2

| TRAJ ANGLE (DEG) | PATH LENGTH (FT) | HORIZ. RANGE (FT) | HEIGHT (FT) | ENERGY (FT-LBS) | VELOCITY (FT/SEC) | TIME (SEC) |
|-------------------------------|------------------|----------------------|---|-----------------|-------------------|------------|
| INITIAL VEL. = 200 6.054 | 381.766 | MASS = 20 380.000 | INITIAL ANGLE = 5.000 # RICOCHETS = 4 28.890 0.654D+04 73.822 2.79901 | | | |
| INITIAL VEL. = 200 -0.871 | 381.813 | MASS = 20 380.000 | INITIAL ANGLE = 7.500 # RICOCHETS = 2 29.354 0.672D+04 100.686 2.58409 | | | |
| INITIAL VEL. = 200 11.934 | 382.173 | MASS = 20 380.000 | INITIAL ANGLE = 10.000 # RICOCHETS = 2 27.909 0.675D+04 74.400 2.54044 | | | |
| INITIAL VEL. = 300 -12.045 | 902.083 | MASS = 20 894.088 | INITIAL ANGLE = 5.000 # RICOCHETS = 6 0.000 0.113D+05 31.880 6.20394 | | | |
| INITIAL VEL. = 300 -22.674 | 908.656 | MASS = 20 899.766 | INITIAL ANGLE = 7.500 # RICOCHETS = 3 0.000 0.102D+05 32.758 5.68059 | | | |
| INITIAL VEL. = 300 -15.074 | 906.747 | MASS = 20 896.732 | INITIAL ANGLE = 10.000 # RICOCHETS = 3 0.000 0.106D+05 30.970 5.80167 | | | |

DO YOU WISH TO SEE THE OUTPUT AGAIN (Y/N) ?

Figure 13: PLOT OF WORKING BARRIER DATA - PROBLEM 2

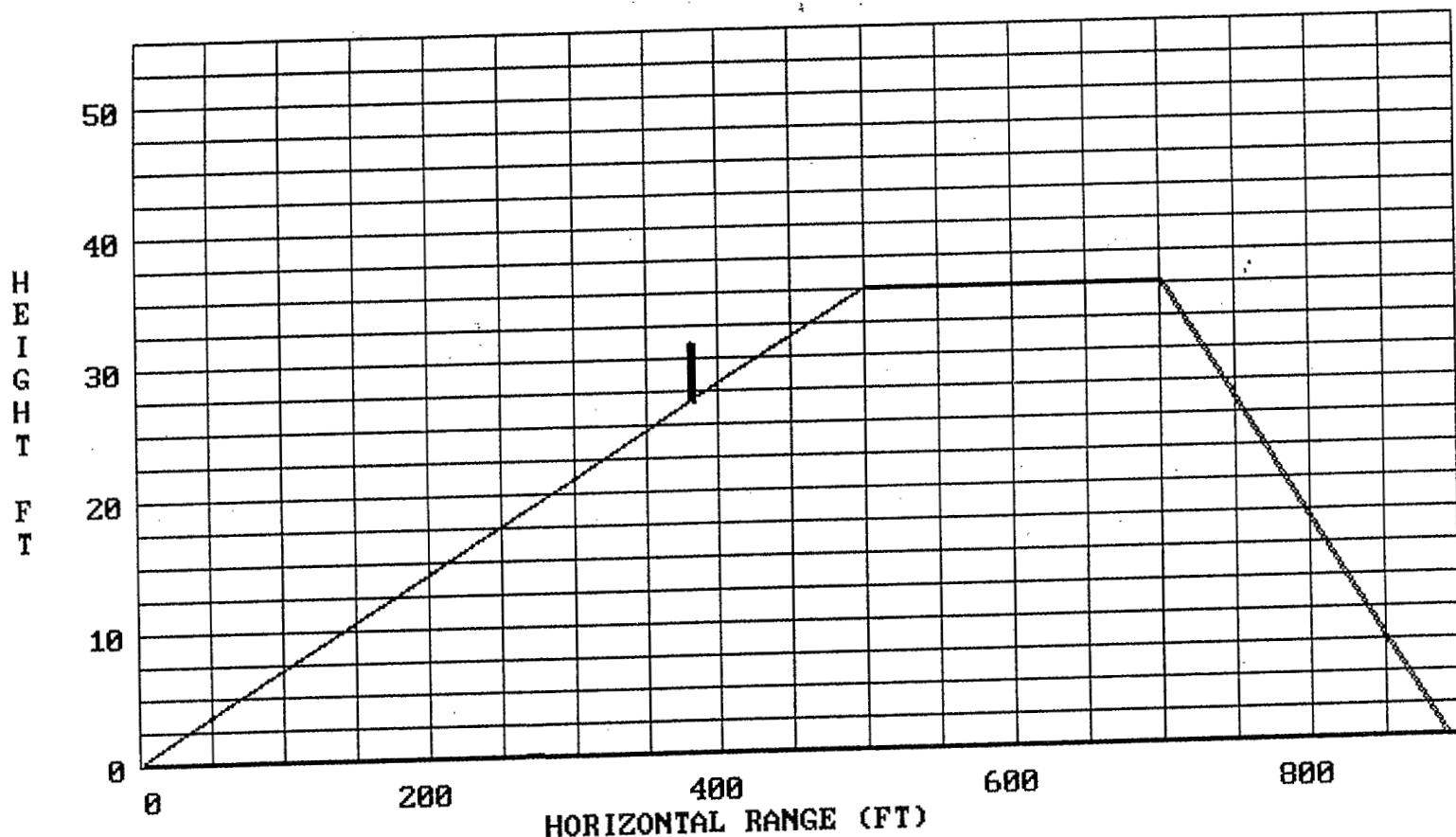


Figure 14: PLOT OF FRAGMENT TRAJECTORIES - PROBLEM 2

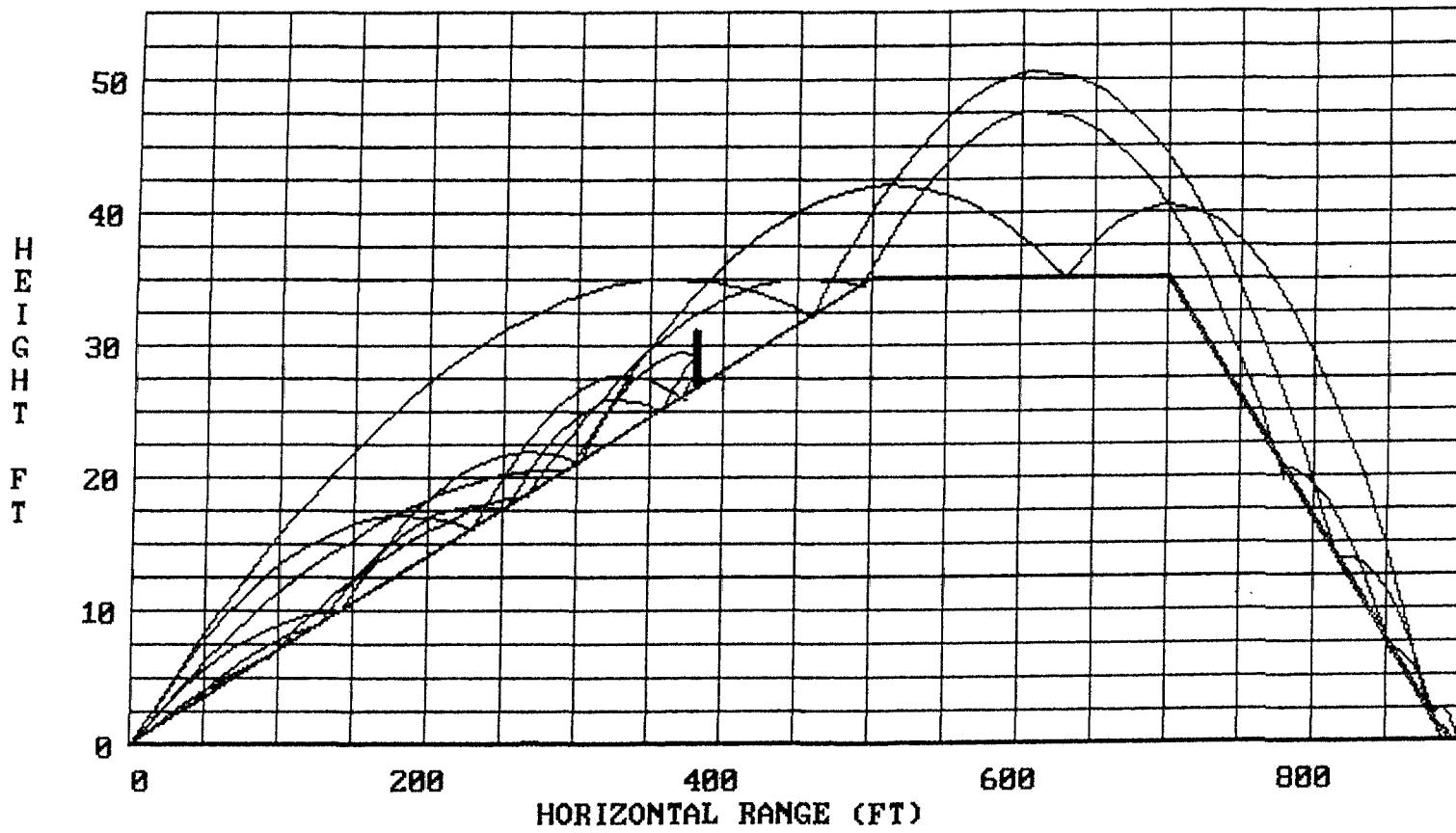


Figure 15: COMPLETE TRAJECTORY CONDITIONS DISPLAY - PROBLEM 2

ANALYTICAL SOLUTION FOR TRAJECTORY WITH VARIABLE DRAG 06-30-1990

SAMPLE RUN

YMIN= 0 NUMBER OF BARRIERS= 4

| | | | |
|---|------------------------------|---------------|-------------|
| 1 | NUMBER OF POINTS= 2 | SOIL CONST= 2 | A= 0 |
| | X1= 0 X2= 500 | X3= 0 | B= .07 |
| | Y1= 0 Y2= 35 | Y3= 0 | C= 0 |
| 2 | NUMBER OF POINTS= 2 | SOIL CONST= 2 | A= 0 |
| | X1= 500 X2= 700 | X3= 0 | B= 0 |
| | Y1= 35 Y2= 35 | Y3= 0 | C= 35 |
| 3 | NUMBER OF POINTS= 2 | SOIL CONST= 2 | A= 0 |
| | X1= 700 X2= 890 | X3= 0 | B=-.1842105 |
| | Y1= 35 Y2= 0 | Y3= 0 | C= 163.9474 |
| 4 | NUMBER OF POINTS= 2 | SOIL CONST= 2 | A= 0 |
| | X1= 380 X2= 380 | X3= 0 | B= 1E+30 |
| | Y1= 27 Y2= 31 | Y3= 0 | C= 0 |

200 VELOCITY # 1
 20 MASS # 1
 5 ANGLE # 1

LENGTH UNIT=FT MASS UNIT=LBS TIME UNIT=SEC ENERGY UNIT=FT-LBS

NUMBER OF (C,U) PAIRS IN THE DRAG COEFFICIENT TABLE = 6
 1.08 4 1.14 2 1.26 1.15 1.09 .9 .88 .75 .8 0

| | | | |
|----------------------------|--------------|---------------------------|---------------|
| FRAGMENT STARTS AT (FT) | X= 0 | Y= 0 | |
| TRAJECTORY LIMITS (FT) | X9= 0 | Y9= 0 | |
| RADIUS OF CURVATURE (FT) | R= 1 | | |
| INITIAL ANGLE (DEG) | A0= 5 | AMB. DENSITY (LBS/CUFT) | D0= 7.647D-02 |
| INITIAL VELOCITY (FT/SEC) | U0= 200 | AMB. SOUND SPEED (FT/SEC) | C0= 1116.45 |
| FRAGMENT MASS (LBS) | M= 20 | GRAVITY (FT/SEC/SEC) | G= 32.174 |
| SHAPE FACTOR | B=0.4600 | DRAG DECAY CONSTANT | C=0.44330D-03 |
| FRAGMENT AREA (SQFT) | A6= 0.437980 | DRAG COEFFICIENT | C1= .8 |
| CHARACTERISTIC LENGTH (FT) | L= 0.661800 | (DRAG IS INTERPOLATED) | |
| FRAG. DENSITY (LBS/CUFT) | D= 150 | STEP SIZE UP (DEG) | I= .5 |
| ENERGY UNIT (FT-LBS) | E5= 32.174 | STEP SIZE DOWN (DEG) | I2= .5 |

| TRAJ ANGLE (DEG) | PATH LENGTH (FT) | HORIZ. RANGE (FT) | HEIGHT (FT) | ENERGY (FT-LBS) | VELOCITY (FT/SEC) | TIME (SEC) |
|------------------------|------------------------|-------------------------|----------------|--------------------|----------------------|---------------|
| 5.000 | 0.000 | 0.000 | 0.000 | 0.124D+05 | 200.000 | 0.00000 |
| 4.500 | 10.798 | 10.761 | 0.894 | 0.122D+05 | 198.380 | 0.05421 |
| 4.000 | 21.417 | 21.351 | 1.682 | 0.120D+05 | 196.813 | 0.10795 |
| 3.500 | 31.865 | 31.776 | 2.365 | 0.119D+05 | 195.297 | 0.16124 |
| 3.000 | 42.149 | 42.043 | 2.948 | 0.117D+05 | 193.829 | 0.21410 |
| 2.981 | 42.539 | 42.433 | 2.969 | 0.117D+05 | 193.774 | 0.21611 |
| 2.986 | 42.439 | 42.333 | 2.963 | 0.117D+05 | 193.788 | 0.21559 |
| 6.476 | 42.439 | 42.334 | 2.963 | 0.117D+05 | 181.456 | 0.21559 |
| 5.828 | 53.967 | 53.795 | 4.199 | 0.115D+05 | 179.811 | 0.27942 |
| 5.181 | 65.277 | 65.053 | 5.284 | 0.113D+05 | 178.231 | 0.34259 |
| 4.533 | 76.381 | 76.117 | 6.225 | 0.111D+05 | 176.712 | 0.40516 |
| 3.886 | 87.290 | 86.996 | 7.026 | 0.109D+05 | 175.253 | 0.46715 |
| 3.238 | 98.014 | 97.699 | 7.692 | 0.107D+05 | 173.850 | 0.52859 |
| 2.590 | 108.563 | 108.234 | 8.229 | 0.105D+05 | 172.501 | 0.58950 |
| 1.943 | 118.945 | 118.608 | 8.640 | 0.104D+05 | 171.204 | 0.64992 |
| 1.295 | 129.171 | 128.830 | 8.929 | 0.102D+05 | 169.958 | 0.70986 |
| 1.432 | 127.023 | 126.682 | 8.877 | 0.103D+05 | 170.217 | 0.69723 |
| 1.419 | 127.234 | 126.893 | 8.883 | 0.103D+05 | 170.191 | 0.69847 |

| | | | | | | |
|--------|---------|---------|--------|-----------|---------|---------|
| 1.418 | 127.239 | 126.898 | 8.883 | 0.103D+05 | 170.191 | 0.69850 |
| 9.078 | 127.239 | 126.898 | 8.883 | 0.103D+05 | 155.814 | 0.69850 |
| 8.170 | 139.203 | 138.727 | 10.677 | 0.101D+05 | 154.176 | 0.77569 |
| 7.262 | 150.896 | 150.313 | 12.248 | 0.985D+04 | 152.623 | 0.85192 |
| 6.354 | 162.336 | 161.672 | 13.604 | 0.966D+04 | 151.151 | 0.92724 |
| 5.447 | 173.541 | 172.818 | 14.756 | 0.948D+04 | 149.755 | 1.00171 |
| 4.539 | 184.529 | 183.763 | 15.713 | 0.932D+04 | 148.431 | 1.07541 |
| 3.631 | 195.313 | 194.520 | 16.482 | 0.916D+04 | 147.177 | 1.14837 |
| 2.723 | 205.909 | 205.099 | 17.069 | 0.901D+04 | 145.990 | 1.22066 |
| 1.816 | 216.332 | 215.513 | 17.482 | 0.888D+04 | 144.866 | 1.29233 |
| 0.908 | 226.592 | 225.771 | 17.726 | 0.875D+04 | 143.802 | 1.36342 |
| 0.000 | 236.704 | 235.882 | 17.807 | 0.862D+04 | 142.797 | 1.43398 |
| -1.256 | 250.475 | 249.651 | 17.656 | 0.847D+04 | 141.497 | 1.53086 |
| -1.462 | 252.708 | 251.883 | 17.603 | 0.844D+04 | 141.294 | 1.54665 |
| -1.434 | 252.405 | 251.581 | 17.611 | 0.845D+04 | 141.322 | 1.54451 |
| -1.435 | 252.410 | 251.586 | 17.611 | 0.845D+04 | 141.321 | 1.54454 |
| 11.540 | 252.410 | 251.586 | 17.611 | 0.845D+04 | 117.926 | 1.54454 |
| 10.386 | 261.190 | 260.204 | 19.281 | 0.828D+04 | 116.769 | 1.61936 |
| 9.232 | 269.771 | 268.660 | 20.743 | 0.813D+04 | 115.686 | 1.69319 |
| 8.078 | 278.171 | 276.963 | 22.007 | 0.799D+04 | 114.676 | 1.76612 |
| 6.924 | 286.405 | 285.127 | 23.083 | 0.786D+04 | 113.735 | 1.83822 |
| 5.770 | 294.489 | 293.161 | 23.977 | 0.774D+04 | 112.859 | 1.90957 |
| 4.616 | 302.437 | 301.076 | 24.696 | 0.763D+04 | 112.047 | 1.98025 |
| 3.462 | 310.262 | 308.881 | 25.247 | 0.752D+04 | 111.295 | 2.05032 |
| 2.308 | 317.977 | 316.586 | 25.636 | 0.743D+04 | 110.601 | 2.11986 |
| 1.154 | 325.593 | 324.198 | 25.866 | 0.734D+04 | 109.964 | 2.18892 |
| 0.000 | 333.123 | 331.727 | 25.942 | 0.727D+04 | 109.381 | 2.25757 |
| -1.958 | 345.732 | 344.332 | 25.728 | 0.715D+04 | 108.513 | 2.37331 |
| -3.917 | 358.172 | 356.754 | 25.091 | 0.706D+04 | 107.789 | 2.48834 |
| -4.071 | 359.148 | 357.728 | 25.023 | 0.705D+04 | 107.738 | 2.49740 |
| -4.051 | 359.019 | 357.599 | 25.032 | 0.705D+04 | 107.745 | 2.49620 |
| -4.051 | 359.020 | 357.600 | 25.032 | 0.705D+04 | 107.745 | 2.49621 |
| 13.374 | 359.020 | 357.600 | 25.032 | 0.705D+04 | 76.625 | 2.49621 |
| 12.037 | 363.351 | 361.825 | 25.985 | 0.694D+04 | 76.000 | 2.55296 |
| 10.700 | 367.593 | 365.983 | 26.821 | 0.683D+04 | 75.428 | 2.60899 |
| 9.362 | 371.756 | 370.082 | 27.546 | 0.674D+04 | 74.906 | 2.66436 |
| 8.025 | 375.848 | 374.127 | 28.165 | 0.665D+04 | 74.433 | 2.71916 |
| 6.687 | 379.877 | 378.123 | 28.681 | 0.658D+04 | 74.007 | 2.77345 |
| 6.055 | 381.761 | 379.995 | 28.890 | 0.654D+04 | 73.822 | 2.79895 |
| 6.054 | 381.766 | 380.000 | 28.890 | 0.654D+04 | 73.822 | 2.79901 |

NO. OF RICOCHETS = 4

AVE. DRAG COEFF. = 3.123498 AVE. DRAG DECAY CONST. = 1.730826E-03

X(APPROX.) = 91.1522 Q= .6876818

X(CORCTD.) = 107.9432 Q= 6.383077E-12

FINAL VALUES.....X = 380 Y = 28.89038

200 VELOCITY # 1
20 MASS # 1
7.5 ANGLE # 2

LENGTH UNIT=FT MASS UNIT=LBS TIME UNIT=SEC ENERGY UNIT=FT-LBS

NUMBER OF (C,U) PAIRS IN THE DRAG COEFFICIENT TABLE = 6

| 1.08 | 4 | 1.14 | 2 | 1.26 | 1.15 | 1.09 | .9 | .88 | .75 | .8 | 0 |
|------|---|------|---|------|------|------|----|-----|-----|----|---|
|------|---|------|---|------|------|------|----|-----|-----|----|---|

FRAGMENT STARTS AT (FT) X= 0 Y= 0

TRAJECTORY LIMITS (FT) X9= 0 Y9= 0

RADIUS OF CURVATURE (FT) R= 1

INITIAL ANGLE (DEG) A0= 7.5 AMB. DENSITY (LBS/CUFT) D0= 7.647D-02

INITIAL VELOCITY (FT/SEC) U0= 200 AMB. SOUND SPEED (FT/SEC) C0= 1116.45

FRAGMENT MASS (LBS) M= 20 GRAVITY (FT/SEC/SEC) G= 32.174

SHAPE FACTOR B=0.4600 DRAG DECAY CONSTANT C=0.44330D-03

FRAGMENT AREA (SQFT) A6= 0.437980 DRAG COEFFICIENT C1= .8

CHARACTERISTIC LENGTH (FT) L= 0.661800 (DRAG IS INTERPOLATED)

FRAG. DENSITY (LBS/CUFT) D= 150 STEP SIZE UP (DEG) I= .625

ENERGY UNIT (FT-LBS) E5= 32.174 STEP SIZE DOWN (DEG) I2= .75

| TRAJ ANGLE (DEG) | PATH LENGTH (FT) | HORIZ. RANGE (FT) | HEIGHT (FT) | ENERGY (FT-LBS) | VELOCITY (FT/SEC) | TIME (SEC) |
|------------------|------------------|-------------------|-------------|-----------------|-------------------|------------|
| 7.500 | 0.000 | 0.000 | 0.000 | 0.124D+05 | 200.000 | 0.00000 |
| 6.875 | 13.524 | 13.417 | 1.692 | 0.122D+05 | 197.881 | 0.06798 |
| 6.416 | 23.260 | 23.088 | 2.819 | 0.120D+05 | 196.381 | 0.11737 |
| 5.950 | 33.000 | 32.771 | 3.869 | 0.118D+05 | 194.902 | 0.16715 |
| 5.476 | 42.742 | 42.465 | 4.838 | 0.116D+05 | 193.445 | 0.21733 |
| 4.994 | 52.486 | 52.168 | 5.728 | 0.115D+05 | 192.010 | 0.26788 |
| 4.505 | 62.231 | 61.880 | 6.535 | 0.113D+05 | 190.596 | 0.31883 |
| 4.008 | 71.979 | 71.600 | 7.258 | 0.111D+05 | 189.206 | 0.37015 |
| 3.504 | 81.728 | 81.328 | 7.897 | 0.110D+05 | 187.838 | 0.42187 |
| 2.991 | 91.479 | 91.064 | 8.450 | 0.108D+05 | 186.493 | 0.47397 |
| 2.471 | 101.233 | 100.806 | 8.915 | 0.107D+05 | 185.171 | 0.52645 |
| 1.943 | 110.988 | 110.554 | 9.290 | 0.105D+05 | 183.873 | 0.57932 |
| 1.408 | 120.746 | 120.308 | 9.576 | 0.104D+05 | 182.599 | 0.63258 |
| 0.865 | 130.507 | 130.066 | 9.770 | 0.102D+05 | 181.349 | 0.68621 |
| 0.314 | 140.270 | 139.829 | 9.870 | 0.101D+05 | 180.124 | 0.74023 |
| 0.235 | 141.644 | 141.203 | 9.877 | 0.101D+05 | 179.953 | 0.74786 |
| 0.242 | 141.529 | 141.088 | 9.876 | 0.101D+05 | 179.968 | 0.74723 |
| 0.242 | 141.530 | 141.089 | 9.876 | 0.101D+05 | 179.968 | 0.74723 |
| 10.332 | 141.530 | 141.089 | 9.876 | 0.101D+05 | 159.963 | 0.74723 |
| 9.471 | 153.532 | 152.912 | 11.940 | 0.985D+04 | 158.242 | 0.82266 |
| 8.760 | 163.236 | 162.493 | 13.478 | 0.968D+04 | 156.884 | 0.88425 |
| 8.034 | 172.947 | 172.100 | 14.896 | 0.952D+04 | 155.557 | 0.94642 |
| 7.294 | 182.662 | 181.728 | 16.192 | 0.936D+04 | 154.261 | 1.00913 |
| 6.541 | 192.381 | 191.376 | 17.363 | 0.921D+04 | 152.997 | 1.07239 |
| 5.773 | 202.105 | 201.043 | 18.406 | 0.906D+04 | 151.767 | 1.13620 |
| 4.992 | 211.832 | 210.728 | 19.319 | 0.892D+04 | 150.569 | 1.20055 |
| 4.197 | 221.565 | 220.429 | 20.099 | 0.878D+04 | 149.407 | 1.26544 |
| 3.388 | 231.303 | 230.145 | 20.743 | 0.865D+04 | 148.279 | 1.33087 |
| 2.567 | 241.046 | 239.875 | 21.250 | 0.852D+04 | 147.188 | 1.39682 |
| 1.732 | 250.795 | 249.616 | 21.615 | 0.840D+04 | 146.133 | 1.46329 |
| 0.884 | 260.550 | 259.368 | 21.838 | 0.828D+04 | 145.116 | 1.53028 |
| 0.024 | 270.311 | 269.129 | 21.916 | 0.817D+04 | 144.137 | 1.59777 |
| 0.000 | 270.576 | 269.394 | 21.916 | 0.817D+04 | 144.110 | 1.59961 |
| -1.364 | 285.790 | 284.606 | 21.736 | 0.801D+04 | 142.665 | 1.70571 |
| -2.728 | 300.720 | 299.526 | 21.204 | 0.786D+04 | 141.341 | 1.81085 |
| -2.935 | 302.960 | 301.763 | 21.093 | 0.784D+04 | 141.151 | 1.82671 |
| -2.911 | 302.704 | 301.507 | 21.106 | 0.784D+04 | 141.173 | 1.82490 |
| -2.912 | 302.708 | 301.511 | 21.106 | 0.784D+04 | 141.172 | 1.82492 |
| 12.469 | 302.708 | 301.511 | 21.106 | 0.784D+04 | 108.790 | 1.82492 |
| 11.430 | 309.469 | 308.125 | 22.506 | 0.771D+04 | 107.877 | 1.88733 |
| 9.916 | 319.085 | 317.574 | 24.287 | 0.753D+04 | 106.643 | 1.97699 |
| 8.357 | 328.718 | 327.084 | 25.817 | 0.737D+04 | 105.486 | 2.06781 |
| 6.755 | 338.368 | 336.649 | 27.087 | 0.722D+04 | 104.409 | 2.15976 |
| 5.113 | 348.039 | 346.268 | 28.087 | 0.709D+04 | 103.418 | 2.25283 |
| 3.432 | 357.732 | 355.933 | 28.810 | 0.696D+04 | 102.516 | 2.34697 |
| 1.716 | 367.449 | 365.638 | 29.247 | 0.685D+04 | 101.705 | 2.44213 |
| 0.000 | 377.010 | 375.197 | 29.391 | 0.676D+04 | 101.003 | 2.53646 |
| -0.868 | 381.798 | 379.985 | 29.354 | 0.672D+04 | 100.687 | 2.58394 |
| -0.871 | 381.813 | 380.000 | 29.354 | 0.672D+04 | 100.686 | 2.58409 |

NO. OF RICOCHETS = 2

AVE. DRAG COEFF. = 2.120243 AVE. DRAG DECAY CONST. = 1.174891E-03

X(APPROX.) = 135.421 Q= .6913177

X(CORCTD.) = 160.8871 Q= 1.777936E-08

FINAL VALUES....X = 380 Y = 29.35426

200 VELOCITY # 1
20 MASS # 1
10 ANGLE # 3

LENGTH UNIT=FT MASS UNIT=LBS TIME UNIT=SEC ENERGY UNIT=FT-LBS

NUMBER OF (C,U) PAIRS IN THE DRAG COEFFICIENT TABLE = 6
 1.08 4 1.14 2 1.26 1.15 1.09 .9 .88 .75 .8 0

FRAGMENT STARTS AT (FT) X= 0 Y= 0
 TRAJECTORY LIMITS (FT) X9= 0 Y9= 0
 RADIUS OF CURVATURE (FT) R= 1
 INITIAL ANGLE (DEG) A0= 10 AMB. DENSITY (LBS/CUFT) D0= 7.647D-02
 INITIAL VELOCITY (FT/SEC) U0= 200 AMB. SOUND SPEED (FT/SEC) C0= 1116.45
 FRAGMENT MASS (LBS) M= 20 GRAVITY (FT/SEC/SEC) G= 32.174
 SHAPE FACTOR B=0.4600 DRAG DECAY CONSTANT C=0.44330D-03
 FRAGMENT AREA (SQFT) A6= 0.437980 DRAG COEFFICIENT C1= .8
 CHARACTERISTIC LENGTH (FT) L= 0.661800 (DRAG IS INTERPOLATED)
 FRAG. DENSITY (LBS/CUFT) D= 150 STEP SIZE UP (DEG) I= .625
 ENERGY UNIT (FT-LBS) E5= 32.174 STEP SIZE DOWN (DEG) I2= 1

| TRAJ ANGLE (DEG) | PATH LENGTH (FT) | HORIZ. RANGE (FT) | HEIGHT (FT) | ENERGY (FT-LBS) | VELOCITY (FT/SEC) | TIME (SEC) |
|------------------------|------------------------|-------------------------|----------------|--------------------|----------------------|---------------|
| 10.000 | 0.000 | 0.000 | 0.000 | 0.124D+05 | 200.000 | 0.00000 |
| 9.375 | 13.604 | 13.410 | 2.290 | 0.122D+05 | 197.774 | 0.06840 |
| 8.919 | 23.328 | 23.010 | 3.836 | 0.120D+05 | 196.208 | 0.11776 |
| 8.455 | 33.058 | 32.629 | 5.305 | 0.118D+05 | 194.663 | 0.16755 |
| 7.982 | 42.790 | 42.260 | 6.697 | 0.116D+05 | 193.138 | 0.21774 |
| 7.502 | 52.523 | 51.904 | 8.008 | 0.114D+05 | 191.636 | 0.26833 |
| 7.014 | 62.257 | 61.561 | 9.238 | 0.112D+05 | 190.155 | 0.31932 |
| 6.517 | 71.994 | 71.229 | 10.385 | 0.111D+05 | 188.697 | 0.37072 |
| 6.012 | 81.732 | 80.909 | 11.448 | 0.109D+05 | 187.261 | 0.42253 |
| 5.499 | 91.471 | 90.599 | 12.424 | 0.107D+05 | 185.849 | 0.47474 |
| 4.977 | 101.213 | 100.300 | 13.314 | 0.106D+05 | 184.459 | 0.52735 |
| 4.447 | 110.957 | 110.011 | 14.115 | 0.104D+05 | 183.093 | 0.58037 |
| 3.908 | 120.703 | 119.731 | 14.825 | 0.103D+05 | 181.751 | 0.63380 |
| 3.361 | 130.451 | 129.460 | 15.443 | 0.101D+05 | 180.433 | 0.68763 |
| 2.806 | 140.202 | 139.196 | 15.968 | 0.997D+04 | 179.139 | 0.74186 |
| 2.242 | 149.955 | 148.940 | 16.397 | 0.983D+04 | 177.871 | 0.79650 |
| 1.670 | 159.711 | 158.690 | 16.730 | 0.970D+04 | 176.627 | 0.85154 |
| 1.090 | 169.470 | 168.446 | 16.966 | 0.956D+04 | 175.410 | 0.90698 |
| 0.501 | 179.232 | 178.206 | 17.101 | 0.943D+04 | 174.218 | 0.96282 |
| 0.000 | 187.434 | 186.408 | 17.137 | 0.933D+04 | 173.237 | 1.01004 |
| -1.000 | 203.538 | 202.511 | 16.998 | 0.913D+04 | 171.366 | 1.10350 |
| -2.000 | 219.309 | 218.276 | 16.585 | 0.894D+04 | 169.606 | 1.19601 |
| -2.871 | 232.790 | 231.745 | 16.013 | 0.879D+04 | 168.159 | 1.27583 |
| -2.749 | 230.927 | 229.884 | 16.104 | 0.881D+04 | 168.356 | 1.26476 |
| -2.756 | 231.032 | 229.989 | 16.099 | 0.881D+04 | 168.345 | 1.26538 |
| 12.364 | 231.032 | 229.990 | 16.099 | 0.881D+04 | 130.978 | 1.26538 |
| 11.591 | 238.326 | 237.125 | 17.613 | 0.867D+04 | 129.957 | 1.32129 |
| 10.546 | 247.984 | 246.602 | 19.468 | 0.850D+04 | 128.647 | 1.39598 |
| 9.475 | 257.652 | 256.123 | 21.149 | 0.833D+04 | 127.382 | 1.47150 |
| 8.378 | 267.328 | 265.681 | 22.650 | 0.817D+04 | 126.167 | 1.54783 |
| 7.257 | 277.013 | 275.276 | 23.968 | 0.802D+04 | 125.003 | 1.62495 |
| 6.111 | 286.708 | 284.904 | 25.097 | 0.788D+04 | 123.891 | 1.70285 |
| 4.940 | 296.413 | 294.564 | 26.032 | 0.775D+04 | 122.833 | 1.78153 |
| 3.747 | 306.129 | 304.251 | 26.768 | 0.762D+04 | 121.832 | 1.86095 |
| 2.531 | 315.857 | 313.964 | 27.301 | 0.750D+04 | 120.888 | 1.94111 |
| 1.294 | 325.598 | 323.699 | 27.627 | 0.739D+04 | 120.004 | 2.02198 |
| 0.037 | 335.352 | 333.451 | 27.740 | 0.729D+04 | 119.181 | 2.10354 |
| 0.000 | 335.635 | 333.734 | 27.740 | 0.729D+04 | 119.158 | 2.10591 |
| -1.845 | 349.719 | 347.815 | 27.515 | 0.716D+04 | 118.084 | 2.22465 |
| -3.691 | 363.582 | 361.660 | 26.846 | 0.705D+04 | 117.160 | 2.34250 |
| -5.428 | 376.473 | 374.509 | 25.822 | 0.696D+04 | 116.420 | 2.45289 |
| -5.070 | 373.830 | 371.877 | 26.064 | 0.698D+04 | 116.562 | 2.43020 |
| -5.097 | 374.032 | 372.078 | 26.046 | 0.697D+04 | 116.551 | 2.43193 |
| -5.098 | 374.035 | 372.082 | 26.046 | 0.697D+04 | 116.551 | 2.43196 |
| 14.530 | 374.035 | 372.082 | 26.046 | 0.697D+04 | 75.611 | 2.43196 |

| | | | | | | |
|--------|---------|---------|--------|-----------|--------|---------|
| 13.622 | 376.922 | 374.881 | 26.748 | 0.689D+04 | 75.165 | 2.47025 |
| 10.581 | 386.283 | 384.031 | 28.712 | 0.665D+04 | 73.845 | 2.59589 |
| 11.944 | 382.142 | 379.970 | 27.903 | 0.675D+04 | 74.404 | 2.54003 |
| 11.934 | 382.173 | 380.000 | 27.909 | 0.675D+04 | 74.400 | 2.54044 |

NO. OF RICOCHETS = 2
 AVE. DRAG COEFF. = 3.11069 AVE. DRAG DECAY CONST. = 1.723728E-03
 X(APPROX.) = 157.1988 Q= .6930333
 X(CORCTD.) = 212.6061 Q= 3.415425E-06
 FINAL VALUES....X = 380 Y = 27.9093

300 VELOCITY # 2
 20 MASS # 1
 5 ANGLE # 1

LENGTH UNIT=FT MASS UNIT=LBS TIME UNIT=SEC ENERGY UNIT=FT-LBS

NUMBER OF (C,U) PAIRS IN THE DRAG COEFFICIENT TABLE = 6
 1.08 4 1.14 2 1.26 1.15 1.09 .9 .88 .75 .8 0

FRAGMENT STARTS AT (FT) X= 0 Y= 0
 TRAJECTORY LIMITS (FT) X9= 0 Y9= 0
 RADIUS OF CURVATURE (FT) R= 1
 INITIAL ANGLE (DEG) A0= 5 AMB. DENSITY (LBS/CUFT) D0= 7.647D-02
 INITIAL VELOCITY (FT/SEC) U0= 300 AMB. SOUND SPEED (FT/SEC) C0= 1116.45
 FRAGMENT MASS (LBS) M= 20 GRAVITY (FT/SEC/SEC) G= 32.174
 SHAPE FACTOR B=0.4600 DRAG DECAY CONSTANT C=0.44330D-03
 FRAGMENT AREA (SQFT) A6= 0.437980 DRAG COEFFICIENT C1= .8
 CHARACTERISTIC LENGTH (FT) L= 0.661800 (DRAG IS INTERPOLATED)
 FRAG. DENSITY (LBS/CUFT) D= 150 STEP SIZE UP (DEG) I= .4166667
 ENERGY UNIT (FT-LBS) E5= 32.174 STEP SIZE DOWN (DEG) I2= .5

| TRAJ ANGLE (DEG) | PATH LENGTH (FT) | HORIZ. RANGE (FT) | HEIGHT (FT) | ENERGY (FT-LBS) | VELOCITY (FT/SEC) | TIME (SEC) |
|------------------------|------------------------|-------------------------|----------------|--------------------|----------------------|---------------|
| 5.000 | 0.000 | 0.000 | 0.000 | 0.280D+05 | 300.000 | 0.00000 |
| 4.583 | 20.118 | 20.047 | 1.681 | 0.272D+05 | 295.661 | 0.06755 |
| 4.377 | 29.852 | 29.751 | 2.441 | 0.268D+05 | 293.589 | 0.10059 |
| 4.168 | 39.609 | 39.482 | 3.168 | 0.264D+05 | 291.530 | 0.13394 |
| 3.955 | 49.367 | 49.215 | 3.860 | 0.260D+05 | 289.489 | 0.16753 |
| 3.739 | 59.125 | 58.951 | 4.514 | 0.257D+05 | 287.465 | 0.20135 |
| 3.521 | 68.883 | 68.689 | 5.132 | 0.253D+05 | 285.459 | 0.23542 |
| 3.299 | 78.642 | 78.431 | 5.713 | 0.250D+05 | 283.470 | 0.26972 |
| 3.074 | 88.401 | 88.175 | 6.255 | 0.246D+05 | 281.499 | 0.30427 |
| 2.939 | 94.175 | 93.941 | 6.558 | 0.244D+05 | 280.342 | 0.32482 |
| 2.963 | 93.152 | 92.920 | 6.505 | 0.245D+05 | 280.546 | 0.32118 |
| 2.962 | 93.207 | 92.974 | 6.508 | 0.245D+05 | 280.535 | 0.32137 |
| 6.526 | 93.207 | 92.975 | 6.508 | 0.245D+05 | 262.629 | 0.32137 |
| 5.983 | 113.373 | 113.021 | 8.706 | 0.237D+05 | 258.726 | 0.39873 |
| 5.714 | 123.099 | 122.696 | 9.697 | 0.234D+05 | 256.871 | 0.43646 |
| 5.441 | 132.851 | 132.402 | 10.645 | 0.231D+05 | 255.029 | 0.47456 |
| 5.164 | 142.603 | 142.113 | 11.546 | 0.227D+05 | 253.204 | 0.51294 |
| 4.882 | 152.357 | 151.828 | 12.400 | 0.224D+05 | 251.397 | 0.55160 |
| 4.597 | 162.111 | 161.549 | 13.206 | 0.221D+05 | 249.608 | 0.59053 |
| 4.307 | 171.865 | 171.274 | 13.964 | 0.218D+05 | 247.836 | 0.62975 |
| 4.013 | 181.620 | 181.003 | 14.671 | 0.215D+05 | 246.082 | 0.66925 |
| 3.715 | 191.376 | 190.736 | 15.329 | 0.212D+05 | 244.347 | 0.70904 |
| 3.412 | 201.132 | 200.474 | 15.935 | 0.209D+05 | 242.629 | 0.74910 |
| 3.105 | 210.889 | 210.215 | 16.490 | 0.206D+05 | 240.929 | 0.78946 |
| 2.793 | 220.647 | 219.960 | 16.992 | 0.203D+05 | 239.247 | 0.83010 |
| 2.477 | 230.405 | 229.708 | 17.441 | 0.200D+05 | 237.584 | 0.87103 |
| 2.156 | 240.164 | 239.459 | 17.835 | 0.197D+05 | 235.939 | 0.91225 |
| 1.831 | 249.925 | 249.213 | 18.175 | 0.195D+05 | 234.312 | 0.95376 |

| | | | | | | |
|---------|---------|---------|--------|-----------|---------|---------|
| 1.501 | 259.686 | 258.970 | 18.459 | 0.192D+05 | 232.703 | 0.99556 |
| 1.226 | 267.732 | 267.014 | 18.650 | 0.190D+05 | 231.391 | 1.03024 |
| 1.256 | 266.851 | 266.133 | 18.631 | 0.190D+05 | 231.534 | 1.02643 |
| 1.255 | 266.891 | 266.173 | 18.632 | 0.190D+05 | 231.528 | 1.02661 |
| 9.282 | 266.891 | 266.173 | 18.632 | 0.190D+05 | 211.240 | 1.02661 |
| 8.508 | 285.560 | 284.618 | 21.520 | 0.185D+05 | 208.109 | 1.11565 |
| 8.096 | 295.269 | 294.225 | 22.922 | 0.182D+05 | 206.510 | 1.16248 |
| 7.676 | 305.006 | 303.869 | 24.258 | 0.179D+05 | 204.926 | 1.20981 |
| 7.249 | 314.743 | 313.524 | 25.523 | 0.176D+05 | 203.363 | 1.25751 |
| 6.815 | 324.482 | 323.190 | 26.715 | 0.174D+05 | 201.820 | 1.30558 |
| 6.374 | 334.223 | 332.866 | 27.034 | 0.171D+05 | 200.297 | 1.35403 |
| 5.925 | 343.964 | 342.551 | 28.878 | 0.168D+05 | 198.796 | 1.40285 |
| 5.470 | 353.707 | 352.246 | 29.845 | 0.166D+05 | 197.315 | 1.45204 |
| 5.007 | 363.452 | 361.950 | 30.735 | 0.163D+05 | 195.856 | 1.50161 |
| 4.537 | 373.198 | 371.662 | 31.546 | 0.161D+05 | 194.419 | 1.55155 |
| 4.059 | 382.946 | 381.383 | 32.276 | 0.159D+05 | 193.003 | 1.60187 |
| 3.574 | 392.696 | 391.110 | 32.925 | 0.156D+05 | 191.610 | 1.65257 |
| 3.082 | 402.447 | 400.845 | 33.492 | 0.154D+05 | 190.239 | 1.70365 |
| 2.579 | 412.260 | 410.646 | 33.976 | 0.152D+05 | 188.882 | 1.75541 |
| 2.056 | 422.312 | 420.690 | 34.383 | 0.150D+05 | 187.517 | 1.80883 |
| 1.513 | 432.611 | 430.984 | 34.704 | 0.148D+05 | 186.144 | 1.86395 |
| 0.947 | 443.162 | 441.533 | 34.931 | 0.145D+05 | 184.765 | 1.92085 |
| 0.359 | 453.973 | 452.342 | 35.054 | 0.143D+05 | 183.381 | 1.97957 |
| 0.000 | 460.492 | 458.861 | 35.074 | 0.142D+05 | 182.561 | 2.01520 |
| -1.312 | 483.836 | 482.202 | 34.809 | 0.138D+05 | 179.714 | 2.14408 |
| -2.052 | 496.702 | 495.063 | 34.432 | 0.135D+05 | 178.207 | 2.21597 |
| -1.922 | 494.460 | 492.822 | 34.510 | 0.136D+05 | 178.466 | 2.20340 |
| -1.929 | 494.578 | 492.940 | 34.506 | 0.136D+05 | 178.452 | 2.20406 |
| -1.929 | 494.579 | 492.941 | 34.506 | 0.136D+05 | 178.452 | 2.20407 |
| 11.842 | 494.579 | 492.941 | 34.506 | 0.136D+05 | 145.395 | 2.20407 |
| 10.855 | 505.992 | 504.130 | 36.752 | 0.133D+05 | 143.770 | 2.28300 |
| 9.771 | 518.204 | 516.144 | 38.939 | 0.130D+05 | 142.089 | 2.36845 |
| 8.630 | 530.713 | 528.492 | 40.940 | 0.127D+05 | 140.429 | 2.45700 |
| 7.429 | 543.531 | 541.183 | 42.731 | 0.124D+05 | 138.798 | 2.54881 |
| 6.167 | 556.668 | 554.226 | 44.286 | 0.121D+05 | 137.201 | 2.64400 |
| 4.839 | 570.133 | 567.628 | 45.579 | 0.118D+05 | 135.646 | 2.74270 |
| 3.444 | 583.937 | 581.396 | 46.576 | 0.115D+05 | 134.140 | 2.84504 |
| 1.979 | 598.094 | 595.536 | 47.247 | 0.113D+05 | 132.693 | 2.95115 |
| 0.443 | 612.616 | 610.053 | 47.555 | 0.111D+05 | 131.314 | 3.06116 |
| 0.000 | 616.749 | 614.186 | 47.571 | 0.110D+05 | 130.942 | 3.09268 |
| -2.140 | 636.403 | 633.834 | 47.206 | 0.107D+05 | 129.293 | 3.24373 |
| -4.280 | 655.626 | 653.022 | 46.132 | 0.105D+05 | 127.881 | 3.39322 |
| -6.421 | 674.514 | 671.825 | 44.373 | 0.103D+05 | 126.691 | 3.54161 |
| -8.561 | 693.160 | 690.309 | 41.944 | 0.101D+05 | 125.711 | 3.68936 |
| -10.701 | 711.650 | 708.536 | 38.852 | 0.100D+05 | 124.930 | 3.83691 |
| -12.841 | 730.069 | 726.564 | 35.096 | 0.992D+04 | 124.340 | 3.98469 |
| -14.981 | 748.497 | 744.449 | 30.667 | 0.986D+04 | 123.933 | 4.13314 |
| -17.122 | 767.015 | 762.242 | 25.547 | 0.982D+04 | 123.705 | 4.28270 |
| -19.262 | 785.706 | 779.995 | 19.713 | 0.981D+04 | 123.653 | 4.43382 |
| -18.802 | 781.671 | 776.181 | 21.029 | 0.981D+04 | 123.649 | 4.40119 |
| -18.849 | 782.081 | 776.569 | 20.897 | 0.981D+04 | 123.649 | 4.40450 |
| -18.850 | 782.091 | 776.579 | 20.893 | 0.981D+04 | 123.649 | 4.40459 |
| -0.715 | 782.091 | 776.579 | 20.893 | 0.981D+04 | 85.405 | 4.40459 |
| -2.968 | 790.967 | 785.448 | 20.609 | 0.972D+04 | 85.001 | 4.50875 |
| -5.221 | 799.790 | 794.247 | 19.979 | 0.966D+04 | 84.733 | 4.61272 |
| -7.474 | 808.603 | 803.005 | 19.005 | 0.963D+04 | 84.599 | 4.71682 |
| -9.727 | 817.448 | 811.748 | 17.682 | 0.963D+04 | 84.596 | 4.82137 |
| -11.980 | 826.366 | 820.505 | 16.003 | 0.966D+04 | 84.723 | 4.92670 |
| -14.233 | 835.399 | 829.301 | 13.955 | 0.972D+04 | 84.982 | 5.03316 |
| -16.486 | 844.593 | 838.165 | 11.520 | 0.980D+04 | 85.372 | 5.14110 |
| -18.740 | 853.995 | 847.124 | 8.675 | 0.993D+04 | 85.896 | 5.25089 |
| -20.195 | 860.202 | 852.975 | 6.606 | 0.100D+05 | 86.308 | 5.32298 |
| -19.882 | 858.857 | 851.712 | 7.067 | 0.100D+05 | 86.215 | 5.30739 |
| -19.901 | 858.939 | 851.789 | 7.039 | 0.100D+05 | 86.220 | 5.30834 |
| -19.901 | 858.941 | 851.791 | 7.039 | 0.100D+05 | 86.220 | 5.30836 |
| 0.589 | 858.941 | 851.791 | 7.039 | 0.100D+05 | 53.923 | 5.30836 |
| 0.540 | 859.018 | 851.868 | 7.039 | 0.100D+05 | 53.920 | 5.30980 |
| 0.000 | 859.869 | 852.718 | 7.043 | 0.999D+04 | 53.886 | 5.32557 |
| -2.155 | 863.257 | 856.106 | 6.980 | 0.996D+04 | 53.802 | 5.38850 |

| | | | | | | |
|---------|---------|---------|--------|-----------|--------|---------|
| -4.309 | 866.644 | 859.487 | 6.789 | 0.995D+04 | 53.793 | 5.45147 |
| -6.464 | 870.045 | 862.872 | 6.470 | 0.998D+04 | 53.860 | 5.51465 |
| -8.618 | 873.474 | 866.271 | 6.020 | 0.100D+05 | 54.004 | 5.57822 |
| -10.773 | 876.945 | 869.692 | 5.435 | 0.101D+05 | 54.225 | 5.64237 |
| -12.927 | 880.476 | 873.146 | 4.710 | 0.102D+05 | 54.525 | 5.70730 |
| -15.082 | 884.081 | 876.644 | 3.837 | 0.104D+05 | 54.905 | 5.77319 |
| -17.236 | 887.780 | 880.196 | 2.808 | 0.105D+05 | 55.369 | 5.84027 |
| -19.391 | 891.591 | 883.813 | 1.610 | 0.108D+05 | 55.918 | 5.90877 |
| -21.280 | 895.041 | 887.048 | 0.411 | 0.110D+05 | 56.474 | 5.97016 |
| -20.868 | 894.280 | 886.338 | 0.685 | 0.109D+05 | 56.347 | 5.95667 |
| -20.897 | 894.334 | 886.388 | 0.666 | 0.109D+05 | 56.356 | 5.95763 |
| 2.299 | 894.334 | 886.389 | 0.665 | 0.109D+05 | 31.366 | 5.95763 |
| 2.108 | 894.436 | 886.491 | 0.669 | 0.109D+05 | 31.360 | 5.96089 |
| 0.000 | 895.559 | 887.614 | 0.690 | 0.109D+05 | 31.315 | 5.99672 |
| -1.200 | 896.197 | 888.252 | 0.683 | 0.109D+05 | 31.308 | 6.01710 |
| -2.400 | 896.836 | 888.890 | 0.663 | 0.109D+05 | 31.316 | 6.03750 |
| -3.600 | 897.476 | 889.529 | 0.630 | 0.109D+05 | 31.337 | 6.05792 |
| -4.800 | 898.117 | 890.169 | 0.583 | 0.109D+05 | 31.371 | 6.07838 |
| -6.001 | 898.762 | 890.810 | 0.522 | 0.110D+05 | 31.420 | 6.09891 |
| -7.201 | 899.410 | 891.454 | 0.447 | 0.110D+05 | 31.482 | 6.11952 |
| -8.401 | 900.063 | 892.101 | 0.359 | 0.111D+05 | 31.559 | 6.14023 |
| -9.601 | 900.721 | 892.751 | 0.256 | 0.111D+05 | 31.650 | 6.16106 |
| -10.801 | 901.386 | 893.405 | 0.138 | 0.112D+05 | 31.755 | 6.18203 |
| -12.001 | 902.058 | 894.064 | 0.005 | 0.113D+05 | 31.875 | 6.20316 |
| -12.045 | 902.083 | 894.088 | -0.000 | 0.113D+05 | 31.880 | 6.20394 |

NO. OF RICOCHETS = 6

AVE. DRAG COEFF. = 2.992448 AVE. DRAG DECAY CONST. = 1.658206E-03

X(APPROX.) = 283.3488 Q= .6987873

X(CORCTD.) = 485.7435 Q= 1.306406E-06

FINAL VALUES....X = 894.0885 Y = 0

INITIAL ANGLE SENSITIVITY: dx/dA = 95.53631

INITIAL VELOCITY SENSITIVITY: dx/dU = 3.238276

INITIAL HEIGHT SENSITIVITY: dx/dY = 11.42999

CYLINDRICAL AREA INCREASE RATIO = 5473.827

SPHERICAL AREA INCREASE RATIO = 4912781

300 VELOCITY # 2
20 MASS # 1
7.5 ANGLE # 2

LENGTH UNIT=FT MASS UNIT=LBS TIME UNIT=SEC ENERGY UNIT=FT-LBS

NUMBER OF (C,U) PAIRS IN THE DRAG COEFFICIENT TABLE = 6

| | | | | | | | | | | | |
|------|---|------|---|------|------|------|----|-----|-----|----|---|
| 1.08 | 4 | 1.14 | 2 | 1.26 | 1.15 | 1.09 | .9 | .88 | .75 | .8 | 0 |
|------|---|------|---|------|------|------|----|-----|-----|----|---|

FRAGMENT STARTS AT (FT) X= 0 Y= 0

TRAJECTORY LIMITS (FT) X9= 0 Y9= 0

RADIUS OF CURVATURE (FT) R= 1

INITIAL ANGLE (DEG) A0= 7.5 AMB. DENSITY (LBS/CUFT) D0= 7.647D-02

INITIAL VELOCITY (FT/SEC) U0= 300 AMB. SOUND SPEED (FT/SEC) C0= 1116.45

FRAGMENT MASS (LBS) M= 20 GRAVITY (FT/SEC/SEC) G= 32.174
SHAPE FACTOR B=0.4600 DRAG DECAY CONSTANT C=0.44330D-03

FRAGMENT AREA (SQFT) A6= 0.437980 DRAG COEFFICIENT C1= .8

CHARACTERISTIC LENGTH (FT) L= 0.661800 (DRAG IS INTERPOLATED)

FRAG. DENSITY (LBS/CUFT) D= 150 STEP SIZE UP (DEG) I= .4166667

ENERGY UNIT (FT-LBS) E5= 32.174 STEP SIZE DOWN (DEG) I2= .75

| TRAJ ANGLE (DEG) | PATH LENGTH (FT) | HORIZ. RANGE (FT) | HEIGHT (FT) | ENERGY (FT-LBS) | VELOCITY (FT/SEC) | TIME (SEC) |
|------------------|------------------|-------------------|-------------|-----------------|-------------------|------------|
| 7.500 | 0.000 | 0.000 | 0.000 | 0.280D+05 | 300.000 | 0.00000 |
| 7.083 | 20.203 | 20.040 | 2.565 | 0.271D+05 | 295.549 | 0.06785 |

| | | | | | | |
|--------|---------|---------|--------|-----------|---------|---------|
| 6.878 | 29.930 | 29.694 | 3.747 | 0.268D+05 | 293.433 | 0.10088 |
| 6.669 | 39.683 | 39.379 | 4.897 | 0.264D+05 | 291.330 | 0.13423 |
| 6.457 | 49.436 | 49.068 | 6.012 | 0.260D+05 | 289.244 | 0.16783 |
| 6.242 | 59.189 | 58.761 | 7.091 | 0.256D+05 | 287.175 | 0.20167 |
| 6.024 | 68.942 | 68.459 | 8.133 | 0.253D+05 | 285.125 | 0.23576 |
| 5.802 | 78.696 | 78.161 | 9.138 | 0.249D+05 | 283.091 | 0.27009 |
| 5.577 | 88.450 | 87.867 | 10.105 | 0.246D+05 | 281.076 | 0.30467 |
| 5.349 | 98.205 | 97.577 | 11.034 | 0.242D+05 | 279.078 | 0.33949 |
| 5.118 | 107.959 | 107.291 | 11.924 | 0.239D+05 | 277.097 | 0.37457 |
| 4.883 | 117.714 | 117.009 | 12.774 | 0.235D+05 | 275.134 | 0.40990 |
| 4.644 | 127.470 | 126.730 | 13.584 | 0.232D+05 | 273.188 | 0.44548 |
| 4.402 | 137.226 | 136.456 | 14.354 | 0.229D+05 | 271.261 | 0.48132 |
| 4.157 | 146.982 | 146.185 | 15.082 | 0.225D+05 | 269.350 | 0.51742 |
| 3.908 | 156.739 | 155.917 | 15.768 | 0.222D+05 | 267.457 | 0.55377 |
| 3.655 | 166.496 | 165.653 | 16.411 | 0.219D+05 | 265.582 | 0.59038 |
| 3.399 | 176.253 | 175.392 | 17.012 | 0.216D+05 | 263.724 | 0.62725 |
| 3.139 | 186.012 | 185.135 | 17.568 | 0.213D+05 | 261.884 | 0.66438 |
| 2.875 | 195.770 | 194.880 | 18.080 | 0.210D+05 | 260.062 | 0.70177 |
| 2.607 | 205.529 | 204.628 | 18.547 | 0.207D+05 | 258.257 | 0.73943 |
| 2.336 | 215.289 | 214.379 | 18.968 | 0.204D+05 | 256.470 | 0.77735 |
| 2.061 | 225.050 | 224.132 | 19.342 | 0.202D+05 | 254.701 | 0.81554 |
| 1.782 | 234.811 | 233.887 | 19.670 | 0.199D+05 | 252.949 | 0.85399 |
| 1.499 | 244.572 | 243.645 | 19.949 | 0.196D+05 | 251.216 | 0.89272 |
| 1.212 | 254.335 | 253.404 | 20.180 | 0.193D+05 | 249.500 | 0.93171 |
| 0.920 | 264.098 | 263.166 | 20.362 | 0.191D+05 | 247.802 | 0.97097 |
| 0.625 | 273.861 | 272.929 | 20.494 | 0.188D+05 | 246.122 | 1.01051 |
| 0.326 | 283.626 | 282.693 | 20.575 | 0.186D+05 | 244.459 | 1.05032 |
| 0.023 | 293.391 | 292.458 | 20.605 | 0.183D+05 | 242.815 | 1.09040 |
| 0.000 | 294.125 | 293.191 | 20.605 | 0.183D+05 | 242.692 | 1.09342 |
| -0.037 | 295.290 | 294.357 | 20.604 | 0.183D+05 | 242.498 | 1.09822 |
| -0.036 | 295.282 | 294.349 | 20.604 | 0.183D+05 | 242.499 | 1.09819 |
| 10.568 | 295.282 | 294.349 | 20.604 | 0.183D+05 | 213.678 | 1.09819 |
| 9.981 | 309.885 | 308.718 | 23.209 | 0.178D+05 | 211.152 | 1.16694 |
| 9.581 | 319.608 | 318.299 | 24.861 | 0.176D+05 | 209.495 | 1.21317 |
| 9.175 | 329.341 | 327.901 | 26.447 | 0.173D+05 | 207.856 | 1.25981 |
| 8.761 | 339.074 | 337.515 | 27.965 | 0.170D+05 | 206.237 | 1.30682 |
| 8.341 | 348.808 | 347.141 | 29.412 | 0.168D+05 | 204.638 | 1.35420 |
| 7.913 | 358.543 | 356.779 | 30.789 | 0.165D+05 | 203.059 | 1.40196 |
| 7.479 | 368.279 | 366.427 | 32.093 | 0.163D+05 | 201.500 | 1.45009 |
| 7.037 | 378.017 | 376.087 | 33.323 | 0.160D+05 | 199.962 | 1.49860 |
| 6.588 | 387.756 | 385.757 | 34.478 | 0.158D+05 | 198.445 | 1.54749 |
| 6.131 | 397.496 | 395.437 | 35.557 | 0.155D+05 | 196.949 | 1.59676 |
| 5.667 | 407.238 | 405.127 | 36.559 | 0.153D+05 | 195.475 | 1.64641 |
| 5.187 | 417.156 | 415.001 | 37.497 | 0.151D+05 | 193.996 | 1.69734 |
| 4.687 | 427.316 | 425.123 | 38.371 | 0.148D+05 | 192.504 | 1.74991 |
| 4.167 | 437.724 | 435.500 | 39.175 | 0.146D+05 | 191.002 | 1.80419 |
| 3.625 | 448.386 | 446.137 | 39.900 | 0.144D+05 | 189.490 | 1.86023 |
| 3.061 | 459.309 | 457.041 | 40.537 | 0.141D+05 | 187.969 | 1.91811 |
| 2.473 | 470.498 | 468.217 | 41.077 | 0.139D+05 | 186.442 | 1.97788 |
| 1.860 | 481.961 | 479.672 | 41.511 | 0.137D+05 | 184.909 | 2.03962 |
| 1.222 | 493.706 | 491.412 | 41.827 | 0.135D+05 | 183.373 | 2.10339 |
| 0.557 | 505.738 | 503.442 | 42.014 | 0.132D+05 | 181.836 | 2.16929 |
| 0.000 | 515.660 | 513.364 | 42.062 | 0.131D+05 | 180.597 | 2.22404 |
| -1.429 | 540.519 | 538.219 | 41.755 | 0.126D+05 | 177.606 | 2.36284 |
| -2.858 | 564.604 | 562.286 | 40.857 | 0.122D+05 | 174.867 | 2.49950 |
| -4.286 | 588.007 | 585.641 | 39.401 | 0.119D+05 | 172.359 | 2.63430 |
| -5.715 | 610.809 | 608.355 | 37.415 | 0.116D+05 | 170.064 | 2.76748 |
| -7.144 | 633.086 | 630.491 | 34.923 | 0.113D+05 | 167.966 | 2.89929 |
| -7.099 | 632.394 | 629.804 | 35.008 | 0.113D+05 | 168.029 | 2.89517 |
| -7.103 | 632.463 | 629.872 | 35.000 | 0.113D+05 | 168.022 | 2.89558 |
| 8.596 | 632.463 | 629.872 | 35.000 | 0.113D+05 | 127.939 | 2.89558 |
| 8.119 | 636.731 | 634.095 | 35.620 | 0.112D+05 | 127.412 | 2.92901 |
| 6.378 | 651.960 | 649.200 | 37.543 | 0.109D+05 | 125.613 | 3.04938 |
| 4.528 | 667.651 | 664.818 | 39.036 | 0.106D+05 | 123.898 | 3.17515 |
| 2.572 | 683.755 | 680.889 | 40.035 | 0.103D+05 | 122.290 | 3.30598 |
| 0.509 | 700.293 | 697.418 | 40.481 | 0.101D+05 | 120.806 | 3.44205 |
| 0.000 | 704.310 | 701.435 | 40.499 | 0.100D+05 | 120.472 | 3.47534 |
| -2.202 | 721.459 | 718.578 | 40.171 | 0.980D+04 | 119.164 | 3.61847 |
| -4.404 | 738.291 | 735.379 | 39.203 | 0.963D+04 | 118.071 | 3.76037 |

| | | | | | | |
|---------|---------|---------|--------|-----------|---------|---------|
| -6.606 | 754.892 | 751.900 | 37.612 | 0.948D+04 | 117.180 | 3.90150 |
| -8.809 | 771.343 | 768.200 | 35.407 | 0.937D+04 | 116.483 | 4.04231 |
| -11.011 | 787.721 | 784.331 | 32.590 | 0.929D+04 | 115.970 | 4.18323 |
| -13.213 | 804.103 | 800.345 | 29.153 | 0.923D+04 | 115.637 | 4.32469 |
| -15.415 | 820.563 | 816.291 | 25.085 | 0.921D+04 | 115.479 | 4.46713 |
| -17.617 | 837.178 | 832.217 | 20.362 | 0.921D+04 | 115.492 | 4.61100 |
| -19.819 | 854.025 | 848.171 | 14.956 | 0.924D+04 | 115.675 | 4.75676 |
| -22.021 | 871.187 | 864.198 | 8.829 | 0.929D+04 | 116.027 | 4.90490 |
| -24.224 | 888.750 | 880.347 | 1.933 | 0.938D+04 | 116.549 | 5.05593 |
| -24.310 | 889.449 | 880.984 | 1.646 | 0.938D+04 | 116.573 | 5.06192 |
| -24.302 | 889.386 | 880.927 | 1.671 | 0.938D+04 | 116.571 | 5.06139 |
| 13.388 | 889.386 | 880.927 | 1.671 | 0.938D+04 | 31.476 | 5.06139 |
| 12.644 | 889.795 | 881.326 | 1.763 | 0.932D+04 | 31.373 | 5.07440 |
| 0.000 | 896.355 | 887.804 | 2.492 | 0.880D+04 | 30.478 | 5.28650 |
| -2.249 | 897.488 | 888.937 | 2.469 | 0.880D+04 | 30.478 | 5.32368 |
| -4.497 | 898.624 | 890.072 | 2.403 | 0.882D+04 | 30.525 | 5.36094 |
| -6.746 | 899.770 | 891.211 | 2.290 | 0.888D+04 | 30.620 | 5.39841 |
| -8.995 | 900.930 | 892.360 | 2.132 | 0.896D+04 | 30.762 | 5.43620 |
| -11.243 | 902.109 | 893.521 | 1.924 | 0.907D+04 | 30.954 | 5.47443 |
| -13.492 | 903.315 | 894.698 | 1.666 | 0.922D+04 | 31.196 | 5.51322 |
| -15.741 | 904.553 | 895.896 | 1.353 | 0.939D+04 | 31.491 | 5.55273 |
| -17.989 | 905.831 | 897.119 | 0.983 | 0.960D+04 | 31.841 | 5.59308 |
| -20.238 | 907.156 | 898.371 | 0.549 | 0.985D+04 | 32.248 | 5.63445 |
| -22.487 | 908.538 | 899.657 | 0.045 | 0.101D+05 | 32.717 | 5.67698 |
| -22.674 | 908.656 | 899.766 | -0.000 | 0.102D+05 | 32.758 | 5.68059 |

NO. OF RICOCHETS = 3
 AVE. DRAG COEFF. = 3.005248 AVE. DRAG DECAY CONST. = 1.665299E-03
 X(APPROX.) = 357.5755 Q= .7034488
 X(CORCTD.) = 722.2651 Q= 1.30211E-03
 FINAL VALUES....X = 899.7661 Y = 0
 INITIAL ANGLE SENSITIVITY: dx/dA = 93.3437
 INITIAL VELOCITY SENSITIVITY: dx/dU = 4.797993
 INITIAL HEIGHT SENSITIVITY: dx/dY = 7.550715
 CYLINDRICAL AREA INCREASE RATIO = 5348.2
 SPHERICAL AREA INCREASE RATIO = 4853653

300 VELOCITY # 2
 20 MASS # 1
 10 ANGLE # 3

LENGTH UNIT=FT MASS UNIT=LBS TIME UNIT=SEC ENERGY UNIT=FT-LBS

NUMBER OF (C,U) PAIRS IN THE DRAG COEFFICIENT TABLE = 6
 1.08 4 1.14 2 1.26 1.15 1.09 .9 .88 .75 .8 0

FRAGMENT STARTS AT (FT) X= 0 Y= 0
 TRAJECTORY LIMITS (FT) X9= 0 Y9= 0
 RADIUS OF CURVATURE (FT) R= 1
 INITIAL ANGLE (DEG) A0= 10 AMB. DENSITY (LBS/CUFT) D0= 7.647D-02
 INITIAL VELOCITY (FT/SEC) U0= 300 AMB. SOUND SPEED (FT/SEC) C0= 1116.45
 FRAGMENT MASS (LBS) M= 20 GRAVITY (FT/SEC/SEC) G= 32.174
 SHAPE FACTOR B=0.4600 DRAG DECAY CONSTANT C=0.44330D-03
 FRAGMENT AREA (SQFT) A6= 0.437980 DRAG COEFFICIENT C1= .8
 CHARACTERISTIC LENGTH (FT) L= 0.661800 (DRAG IS INTERPOLATED)
 FRAG. DENSITY (LBS/CUFT) D= 150 STEP SIZE UP (DEG) I= .4166667
 ENERGY UNIT (FT-LBS) E5= 32.174 STEP SIZE DOWN (DEG) I2= 1

| TRAJ ANGLE (DEG) | PATH LENGTH (FT) | HORIZ. RANGE (FT) | HEIGHT (FT) | ENERGY (FT-LBS) | VELOCITY (FT/SEC) | TIME (SEC) |
|------------------------|------------------------|-------------------------|----------------|--------------------|----------------------|---------------|
| 10.000 | 0.000 | 0.000 | 0.000 | 0.280D+05 | 300.000 | 0.00000 |
| 9.583 | 20.328 | 20.031 | 3.458 | 0.271D+05 | 295.427 | 0.06828 |

| | | | | | | |
|---------|---------|---------|--------|-----------|---------|---------|
| 9.379 | 30.047 | 29.618 | 5.059 | 0.267D+05 | 293.269 | 0.10130 |
| 9.172 | 39.795 | 39.238 | 6.630 | 0.263D+05 | 291.121 | 0.13466 |
| 8.961 | 49.543 | 48.865 | 8.166 | 0.260D+05 | 288.990 | 0.16827 |
| 8.747 | 59.292 | 58.497 | 9.667 | 0.256D+05 | 286.878 | 0.20213 |
| 8.529 | 69.040 | 68.135 | 11.131 | 0.252D+05 | 284.782 | 0.23623 |
| 8.308 | 78.789 | 77.779 | 12.558 | 0.248D+05 | 282.705 | 0.27059 |
| 8.084 | 88.538 | 87.428 | 13.948 | 0.245D+05 | 280.644 | 0.30520 |
| 7.856 | 98.288 | 97.084 | 15.300 | 0.241D+05 | 278.602 | 0.34007 |
| 7.625 | 108.037 | 106.744 | 16.613 | 0.238D+05 | 276.576 | 0.37519 |
| 7.391 | 117.787 | 116.411 | 17.887 | 0.234D+05 | 274.568 | 0.41057 |
| 7.152 | 127.537 | 126.082 | 19.121 | 0.231D+05 | 272.578 | 0.44621 |
| 6.911 | 137.288 | 135.759 | 20.315 | 0.228D+05 | 270.605 | 0.48211 |
| 6.665 | 147.039 | 145.442 | 21.468 | 0.224D+05 | 268.649 | 0.51828 |
| 6.416 | 156.790 | 155.129 | 22.578 | 0.221D+05 | 266.711 | 0.55470 |
| 6.163 | 166.541 | 164.822 | 23.647 | 0.218D+05 | 264.791 | 0.59140 |
| 5.906 | 176.293 | 174.520 | 24.672 | 0.215D+05 | 262.888 | 0.62836 |
| 5.645 | 186.045 | 184.223 | 25.653 | 0.212D+05 | 261.002 | 0.66559 |
| 5.381 | 195.798 | 193.931 | 26.590 | 0.209D+05 | 259.135 | 0.70309 |
| 5.112 | 205.551 | 203.643 | 27.482 | 0.206D+05 | 257.284 | 0.74086 |
| 4.840 | 215.305 | 213.360 | 28.328 | 0.203D+05 | 255.452 | 0.77891 |
| 4.563 | 225.059 | 223.081 | 29.128 | 0.200D+05 | 253.637 | 0.81723 |
| 4.282 | 234.814 | 232.807 | 29.880 | 0.197D+05 | 251.840 | 0.85583 |
| 3.997 | 244.570 | 242.537 | 30.584 | 0.194D+05 | 250.060 | 0.89470 |
| 3.708 | 254.325 | 252.271 | 31.240 | 0.192D+05 | 248.298 | 0.93385 |
| 3.415 | 264.082 | 262.008 | 31.846 | 0.189D+05 | 246.555 | 0.97328 |
| 3.118 | 273.839 | 271.750 | 32.402 | 0.186D+05 | 244.829 | 1.01300 |
| 2.816 | 283.597 | 281.494 | 32.908 | 0.184D+05 | 243.121 | 1.05299 |
| 2.510 | 293.356 | 291.242 | 33.361 | 0.181D+05 | 241.431 | 1.09327 |
| 2.199 | 303.115 | 300.993 | 33.762 | 0.179D+05 | 239.759 | 1.13383 |
| 1.884 | 312.875 | 310.747 | 34.110 | 0.176D+05 | 238.105 | 1.17468 |
| 1.565 | 322.636 | 320.504 | 34.404 | 0.174D+05 | 236.470 | 1.21582 |
| 1.241 | 332.398 | 330.263 | 34.643 | 0.171D+05 | 234.853 | 1.25724 |
| 0.912 | 342.161 | 340.024 | 34.826 | 0.169D+05 | 233.254 | 1.29895 |
| 0.579 | 351.925 | 349.787 | 34.954 | 0.167D+05 | 231.674 | 1.34096 |
| 0.242 | 361.689 | 359.551 | 35.024 | 0.165D+05 | 230.112 | 1.38325 |
| 0.000 | 368.599 | 366.461 | 35.038 | 0.163D+05 | 229.018 | 1.41335 |
| -1.000 | 396.513 | 394.372 | 34.797 | 0.157D+05 | 224.695 | 1.53639 |
| -2.000 | 423.417 | 421.267 | 34.095 | 0.151D+05 | 220.676 | 1.65721 |
| -3.000 | 449.409 | 447.233 | 32.963 | 0.146D+05 | 216.933 | 1.77600 |
| -3.571 | 463.882 | 461.682 | 32.134 | 0.144D+05 | 214.909 | 1.84303 |
| -3.514 | 462.435 | 460.237 | 32.223 | 0.144D+05 | 215.110 | 1.83630 |
| -3.516 | 462.486 | 460.288 | 32.220 | 0.144D+05 | 215.103 | 1.83653 |
| 12.914 | 462.486 | 460.288 | 32.220 | 0.144D+05 | 159.220 | 1.83653 |
| 12.376 | 470.015 | 467.634 | 33.868 | 0.142D+05 | 158.071 | 1.88399 |
| 11.547 | 481.373 | 478.746 | 36.223 | 0.139D+05 | 156.370 | 1.95624 |
| 10.677 | 493.011 | 490.165 | 38.466 | 0.136D+05 | 154.671 | 2.03107 |
| 9.763 | 504.931 | 501.896 | 40.582 | 0.133D+05 | 152.978 | 2.10856 |
| 8.803 | 517.142 | 513.946 | 42.552 | 0.130D+05 | 151.294 | 2.18882 |
| 7.795 | 529.651 | 526.323 | 44.358 | 0.127D+05 | 149.624 | 2.27196 |
| 6.736 | 542.467 | 539.036 | 45.980 | 0.124D+05 | 147.974 | 2.35809 |
| 5.625 | 555.599 | 552.092 | 47.394 | 0.121D+05 | 146.347 | 2.44733 |
| 4.458 | 569.058 | 565.497 | 48.578 | 0.119D+05 | 144.751 | 2.53980 |
| 3.234 | 582.852 | 579.260 | 49.504 | 0.116D+05 | 143.191 | 2.63561 |
| 1.950 | 596.994 | 593.386 | 50.144 | 0.114D+05 | 141.674 | 2.73490 |
| 0.605 | 611.494 | 607.881 | 50.468 | 0.112D+05 | 140.208 | 2.83778 |
| 0.000 | 617.915 | 614.303 | 50.502 | 0.111D+05 | 139.588 | 2.88368 |
| -2.042 | 639.205 | 635.586 | 50.125 | 0.108D+05 | 137.666 | 3.03725 |
| -4.085 | 659.973 | 656.320 | 49.018 | 0.105D+05 | 135.993 | 3.18903 |
| -6.127 | 680.322 | 676.586 | 47.209 | 0.103D+05 | 134.550 | 3.33947 |
| -8.169 | 700.349 | 696.454 | 44.719 | 0.101D+05 | 133.323 | 3.48899 |
| -10.212 | 720.142 | 715.990 | 41.560 | 0.993D+04 | 132.300 | 3.63802 |
| -12.254 | 739.785 | 735.254 | 37.735 | 0.981D+04 | 131.471 | 3.78696 |
| -14.297 | 759.361 | 754.305 | 33.241 | 0.971D+04 | 130.828 | 3.93623 |
| -16.339 | 778.950 | 773.194 | 28.068 | 0.964D+04 | 130.363 | 4.08622 |
| -18.381 | 798.629 | 791.975 | 22.197 | 0.960D+04 | 130.071 | 4.23735 |
| -20.424 | 818.480 | 810.695 | 15.604 | 0.958D+04 | 129.947 | 4.39004 |
| -21.070 | 824.812 | 816.617 | 13.360 | 0.958D+04 | 129.943 | 4.43877 |
| -20.982 | 823.945 | 815.807 | 13.672 | 0.958D+04 | 129.943 | 4.43210 |
| -20.984 | 823.970 | 815.830 | 13.663 | 0.958D+04 | 129.943 | 4.43228 |

| | | | | | | |
|---------|---------|---------|--------|-----------|--------|---------|
| 2.475 | 823.970 | 815.830 | 13.663 | 0.958D+04 | 71.500 | 4.43228 |
| 2.372 | 824.256 | 816.116 | 13.675 | 0.957D+04 | 71.481 | 4.43629 |
| 0.000 | 830.794 | 822.652 | 13.811 | 0.947D+04 | 71.105 | 4.52800 |
| -2.265 | 836.986 | 828.841 | 13.689 | 0.941D+04 | 70.863 | 4.61523 |
| -4.530 | 843.155 | 834.998 | 13.323 | 0.937D+04 | 70.735 | 4.70236 |
| -6.796 | 849.331 | 841.142 | 12.714 | 0.937D+04 | 70.717 | 4.78968 |
| -9.061 | 855.542 | 847.293 | 11.857 | 0.939D+04 | 70.810 | 4.87746 |
| -11.326 | 861.819 | 853.469 | 10.746 | 0.945D+04 | 71.013 | 4.96597 |
| -13.591 | 868.192 | 859.691 | 9.371 | 0.953D+04 | 71.328 | 5.05552 |
| -15.857 | 874.694 | 865.978 | 7.719 | 0.965D+04 | 71.758 | 5.14640 |
| -18.122 | 881.359 | 872.351 | 5.771 | 0.979D+04 | 72.303 | 5.23894 |
| -20.387 | 888.225 | 878.832 | 3.507 | 0.998D+04 | 72.970 | 5.33347 |
| -22.652 | 895.334 | 885.443 | 0.899 | 0.102D+05 | 73.761 | 5.43036 |
| -22.748 | 895.642 | 885.728 | 0.780 | 0.102D+05 | 73.798 | 5.43453 |
| -22.739 | 895.610 | 885.699 | 0.792 | 0.102D+05 | 73.794 | 5.43410 |
| 7.114 | 895.610 | 885.699 | 0.792 | 0.102D+05 | 30.363 | 5.43410 |
| 6.817 | 895.760 | 885.847 | 0.810 | 0.102D+05 | 30.341 | 5.43902 |
| 0.000 | 899.132 | 889.207 | 1.012 | 0.100D+05 | 30.058 | 5.55070 |
| -1.499 | 899.867 | 889.942 | 1.002 | 0.100D+05 | 30.054 | 5.57515 |
| -2.999 | 900.603 | 890.677 | 0.973 | 0.100D+05 | 30.070 | 5.59962 |
| -4.498 | 901.341 | 891.413 | 0.925 | 0.100D+05 | 30.106 | 5.62414 |
| -5.998 | 902.082 | 892.152 | 0.857 | 0.101D+05 | 30.164 | 5.64875 |
| -7.497 | 902.829 | 892.894 | 0.769 | 0.101D+05 | 30.242 | 5.67349 |
| -8.997 | 903.583 | 893.640 | 0.661 | 0.102D+05 | 30.342 | 5.69838 |
| -10.496 | 904.346 | 894.392 | 0.532 | 0.103D+05 | 30.463 | 5.72347 |
| -11.995 | 905.119 | 895.150 | 0.381 | 0.104D+05 | 30.606 | 5.74879 |
| -13.495 | 905.905 | 895.916 | 0.208 | 0.105D+05 | 30.771 | 5.77438 |
| -14.994 | 906.704 | 896.690 | 0.011 | 0.106D+05 | 30.960 | 5.80028 |
| -15.074 | 906.747 | 896.732 | -0.000 | 0.106D+05 | 30.970 | 5.80167 |

NO. OF RICOCHETS = 3

AVE. DRAG COEFF. = 3.016831

AVE. DRAG DECAY CONST. = 1.671718E-03

X(APPROX.) = 413.1463 Q= .705964

X(CORCTD.) = 875.3461 Q= 3.902553E-02

FINAL VALUES.....X = 896.7319 Y = 0

INITIAL ANGLE SENSITIVITY: dX/dA = 76.37755

INITIAL VELOCITY SENSITIVITY: dX/dU = 5.330046

INITIAL HEIGHT SENSITIVITY: dX/dY = 4.739301

CYLINDRICAL AREA INCREASE RATIO = 4376.111

SPHERICAL AREA INCREASE RATIO = 3984736